Fiscal Policy and Redistribution: How Government Debt Design Generates Real Effects Without Nominal Rigidities

David C Webb London School of Economics

21 - 08 - 2025

Abstract

This paper develops a dynamic Metzleric model to analyze how fiscal policy and government debt design generate real economic effects in the absence of nominal rigidities. Building on Blanchard's (1986) overlapping generations framework, the model incorporates finite horizons, agent heterogeneity, and incomplete markets to explore redistributive channels of fiscal and monetary interventions. We show that debt-financed tax cuts, changes in debt maturity structure, and inflation targeting all produce real effects by altering household budget sets and intertemporal resource allocation. The paper introduces insurance mechanisms for income and default risk, demonstrating how public debt can be used to smooth shocks and redistribute across cohorts. A second-best welfare theorem is derived, showing that efficient allocations can be decentralized through structured fiscal architecture. The analysis offers an alternative foundation for understanding the long-run impacts of fiscal policy, emphasizing redistribution over nominal frictions.

JEL Classification: E21;E22;E44;E52;E62;H62;H63.

1 Introduction

How do fiscal and monetary policies shape real economic outcomes in a world without nominal rigidities? Conventional macroeconomic models often attribute policy effects to sticky prices, expectations management, or aggregate demand fluctuations. Yet these approaches can obscure a more fundamental mechanism: redistribution. This paper argues that even in a frictionless, forward-looking economy, fiscal and monetary interventions have real consequences. This is because they reallocate resources across time and different types of individual.

The model we propose is a dynamic equilibrium model of consumption and investment decisions with wealth accumulation and a consolidated government budget constraint. The model is in the spirit of Metzler (1951), which was designed to understand how open-market operations have real effects because central bank issuance of money to buy claims on capital reduces private sector receipts from capital, returned to the private sector as tax cuts, but the tax cuts are not fully capitalised, so non-money wealth declines. Households then have to be induced to hold a higher ratio of real money balances to capital, putting downward pressure on interest rates. Savings then increases to rebuild wealth. The price level does not therefore increase to offset the increase in the nominal stock of money as would be the case if the tax cut was fully capitalised. The non-neutrality of this policy can be interpreted as a redistribution of resources from future to current tax payers (see for example Barro (1974)). The maturity structure of government debt and hence debt management policy is not something that can be examined in the essentially static Metzler model, although as Mundell (1965) and others have shown, because of its focus on wealth, it could be adopted to consider some inter-temporal problems in a taxonomic format. This includes highlighting, for example, capital market imperfections and more detail on the burden of the debt.

The Metzler model comprised a savings equals investment relationship (goods market equilibrium), a money market equilibrium and an explicit wealth constraint. It did not include an explicit government budget constraint and did not develop forward looking optimising consumption, asset holding and investment decisions. Let us consider the role of the government budget constraint, which plays a dual role in this paper. In Ricardian regimes, it is treated as an accounting identity, holding ex post for any sequence of fiscal and monetary policies. In contrast, under non-Ricardian regimes, it becomes an equilibrium condition that helps determine the price level. This distinction is central to the analysis that follows, as it underpins the redistributive and real effects of fiscal architecture explored throughout the model. This immediately draws to our attention the notion that fiscal policy can impact real interest rates and the price level. If the government budget constraint is treated as a "uses and sources of funds" condition, then given some predetermined paths for taxes and government expenditure and level of debt finance, the endogenous variable is the path of seigniorage and thereby the path of the future money supply. In this sense, the government budget constraint is satisfied for all policy paths, not as an equilibrium condition.

An alternative view, known as the "fiscal theory of the price level" (see Woodford

(1995) and (2003)), hypotheses that the government's budget constraint is not satisfied for arbitrary price levels but only at equilibrium price levels. In this case the level of nominal government liabilities plays a critical role in determining the price level. Note that, under this theory, the value of government liabilities is equal to the present value of fiscal surpluses and seigniorage payments. Of course, this theory focuses attention on a tension between the ability of the government to borrow more on the basis of an increased value of fiscal surpluses as opposed to the price level satisfying an equilibrium condition. Buiter (2002) has argued that: the government's inter-temporal budget constraint is an accounting identity, not a behavioral or equilibrium condition. It holds for all price levels, so it cannot uniquely determine the price level. Hence using the inter-temporal budget constraint alone to pin down the price level (as some "fiscal theory of the price level interpretations do) is invalid unless embedded in a full model. In short: you can't derive equilibrium prices from an identity you need a model that explains how agents behave and how markets clear. Cochrane (2003) is very explicit about this: "the fiscal theory of the price level" only makes sense within a full equilibrium model. He critiques early formulations that treat the inter-temporal budget constraint as a standalone determinant of prices.¹ The price level adjusts to ensure government solvency, but only within a model that includes household optimization, monetary policy rules, fiscal policy paths and market clearing conditions.

Our principal focus is on fiscal policy. While the failure of Ricardian equivalence under finite horizons is well-established (Blanchard 1986), this paper's contribution lies in demonstrating how the specific design of fiscal architecture—particularly debt maturity structure and insurance mechanisms determines the magnitude and distributional consequences of these effects. Rather than simply noting that equivalence fails, we develop a comprehensive framework showing how different policy instruments (short versus long-term debt, insurance design, heterogeneous agent interactions) create distinct redistributive channels with quantifiable welfare implications.

Barro (1979) argued that government debt should be long-term to allow the government to smooth taxes, as implied by dynamic Ramsey taxation, insured from shocks including short-term debt roll-over risk. Gale (1990) provides a general analysis of the design of government debt in an OLG framework with incomplete markets, in which the debt instruments perform a role in achieving risk sharing between generations. In the spirit of Gale, Angeletos (2002) constructs an inter-temporal model with incomplete markets, in particular the absence of Arrow Debreu securities, or indeed as many linearly independent traded securities and options as states (see Ross 1976). In his model, the market value of long-term debt varies with equilibrium interest rates. This endogenous variation in the debt burden insures the government against the need to raise either the tax rate or the level of debt when fiscal conditions turn bad, for example during wars. This means that the government can smooth out impacts without testing its sequence of sustainable surpluses. Other authors, notably Gibaud, Nosbusch and Vayanos (2013), have considered the role of short and long-maturities of debt in an OLG framework,

¹See also Leeper (1991) and Sims (1994) for important contributions.

when both one-period and two-period bonds are used to insure against interest rate risk and generations act as clienteles for bonds. When arbitrageurs have limited risk capacity and individuals are sufficiently risk averse, longer-term bond returns include a term premium. Greenwood et al (2015) argue that long-term debt does avoid roll-over risk, but this has to be traded-off against the monetary services and hence lower interest costs of short-term debt.

Our focus in this paper is on the impact of debt financed fiscal policy and the maturity structure of government debt. We will explore these through an inter-temporal Metzleric model with capital accumulation and a government funding channel. The inter-temporal Metzler model is developed embedding household optimisation, including asset allocation in a well-known framework due to Blanchard (1986) with a government budget constraint. Individuals have infinite horizons but finite-life expectancy. The framework employed also owes some elements to the extension of Blanchard's model due to Buiter (1988), which elaborates and extends Blanchard's model to include richer demographic dynamics, in particular differential birth and death rates, and more on productivity growth. In the model presented, although individuals hold assets, including fiat money directly, they insure against leaving unplanned bequests by trading annuity contracts. The model compares long-run equilibria across different fiscal setups.

An extended version of the model allows for borrowing and lending, with the default risk on loans being insured, with premia on loans being equivalent to default risk in loan rates. This creates a wedge between borrowing and lending rates but allows for the capitalisation of wage income at the same rate for borrowers and lenders. A final extension of the model is the introduction of simple income shocks to consumers' budgets. Again, we assume that individuals want to insure against these to smooth out their impact. The insurance mechanism proposed to address this issue places demands upon the design of public debt. The government provides partial insurance against income shocks, affecting liquidity needs. Government debt has varying maturities, influencing inter-temporal redistribution. The policies considered are debt financed tax cuts, variations in the composition of government debt and changes in the inflation target. The exercises are purely qualitative and are undertake for comparative steady states that abstract from transitional dynamics. The real impacts of the policy changes all follow from individual household budgets not consolidating the government's budget in an invariant way.

In summary, the model in the paper builds on the established Blanchard (1986) framework where finite horizons break Ricardian neutrality. The extensions focus on three novel dimensions: first, how debt maturity composition affects the timing and distribution of tax burdens across cohorts; second, how government debt can provide insurance against fiscal and income shocks through optimal portfolio design; and third, how agent heterogeneity (patient versus impatient types) amplifies these redistributive mechanisms through borrowing and lending channels.

The paper proceeds as follows. Section 2 introduces the agents and their optimization problems. Section 3 outlines the market equilibrium conditions. Section 4 explores the redistributive effects of fiscal and monetary policy, including Ricardian equivalence,

debt maturity, and inflation targeting. Section 5 extends the model to include agent heterogeneity and borrowing constraints. Section 6 analyzes how public debt can be used to insure against fiscal and income shocks. Section 7 evaluates the efficiency properties of the model and derives a second-best welfare theorem. Section 8 concludes by highlighting the implications for policy design and macroeconomic theory.

Throughout the paper, the government budget constraint plays a dual role. In Ricardian regimes, it is treated as an accounting identity that holds ex post for any sequence of fiscal and monetary policies. In contrast, under non-Ricardian regimes—where fiscal policy is active and monetary policy is passive—the budget constraint becomes an equilibrium condition that helps determine the price level. This distinction is central to the analysis, as it underpins the redistributive effects of debt maturity, tax policy, and inflation targeting explored in later sections.

2 Agents

2.1 Households

We build on Blanchard's (1986) overlapping generations model, where individuals live finite lives but behave as if they have infinite horizons. Each period, a fixed proportion of the population dies and is replaced by new entrants, keeping the population size constant. Individuals earn wages, pay taxes, and face income and mortality risks. At date t, the population is N_t . At each date a proportion $(1 - \gamma)$ of the population die and a proportion $\psi = (1 - \gamma)$ are born, so the population is constant in both size and demographic structure. New-born individuals start to work immediately. Individuals are assumed to supply labour inelastically every period for a wage of $W_{t,s}$ and pay taxes, $T_{t,s}$. At each date a surviving individual suffers a negative temporary shock to wage income (full or partial unemployment) of $\delta W_{t,s}$ with probability v.

In this model, a new-born cohort and all surviving cohorts, regardless of when they were born have the same life expectancy and so face the same optimisation problem. Agents face two risks, at each date they may die with probability $\psi = (1 - \gamma)$. There is also a risk of income loss at each of $\delta W_{t,s}$ with probability v. Individuals invest $A_{t,s}$ in return bearing assets. A a proportion ω is invested in real assets, equities, yielding a return of $(1 + r_t)$ and the remaining proportion, $(1 - \omega)$, in nominal government bonds paying a composite nominal return of return of $(1 + i_t^B)$ or in real terms $(1 + i_t^B) \frac{P_t}{P_{t+1}}$, where P_t is the price level. The total return on on a unit investment in the portfolio is $Z_{t,s} = (1+z_t) = [\omega(1+r_t)+(1-\omega)(1+i_t^B)\frac{P_t}{P_{t+1}}]$ per period. In developing the model, we abstract from return risk and so do not solve for a portfolio rule, ω_t . Individuals can also hold real money balances. To hedge mortality risk individuals also enter into annuity contracts arranged by competitive intermediaries that break even. The annuities avoid

The most general probability distribution is admissible: a probability density over continuous r's, or finite positive probabilities at discrete values of r. In its simplest form, we assume independence between yields at different times so that $F(r_0, r_1, ..., r_t..., r_\infty) = F(r_0)F(r_1)...F(r_t)$. If at each date r_t can take two values with equal probability of $\frac{1}{2}$ of either r_t^h or r_t^l with $r_t^h > (1 + i_t^B) \frac{P_t}{P_{t+1}} - 1 > r_t^l$ and $E_t r_t = \frac{1}{2} r_t^h + \frac{1}{2} r_t^l$.

any unplanned bequests, they pay $(1 - \gamma)Z_{t,s}$ to the survivors from the dyers estates. Hence, the total return in the event of survival at each date is $Z_{t,s}/\gamma$ and zero otherwise. The additional exposure to income losses at every date after the first of $\delta W_{t,s}$ can be hedged by paying premiums to an insurance company. The premiums are paid across periods to smooth consumption. The aggregate present value of these premiums equals the present value of expected payouts. This element of social insurance means that there is sharing of income shocks across cohorts. We will develop the model initially by abstracting from the wage income shocks and their insurance and return to them later in an extended version of the basic model.

Each cohort maximizes lifetime utility, which depends on consumption and real money balances. Preferences for a cohort born at date $s \leq t$ are iso-elastic, defined over consumption and real money balances:

$$U(t,s) = E_s \sum_{t=s}^{\infty} (\beta \gamma)^t \left[\frac{C_{t,s}^{1-\alpha}}{1-\alpha} + \frac{\phi}{1-\sigma} \left(\frac{M_{t,s}}{P_t} \right)^{1-\sigma} \right]$$
 (1)

where $\alpha \geq 0$, and with $\alpha = 1$ is logarithmic utility. The time preference factor is given by $0 < \beta < 1$. The elasticity of marginal utility or coefficient of relative risk aversion parameter, α , balances income and substitution effects, with the income effect reinforcing the substitution effect for $\alpha > 1$. Here, ϕ and σ govern the utility from holding money. This specification is in the spirit of Sidrauski (1967), which sees money as analogous to a durable good yielding a stream of transactions services, but also as a store of value accumulated through savings and competing with other assets. Each cohort faces a budget constraint: current consumption and savings must be financed by asset returns, money holdings, and net income (wages minus taxes). The per period cohort budget constraint is:

$$C_{t,s} + \gamma E_t (\Lambda_{t,t+1} \frac{Z_{t+1} A_{t+1,s}}{\gamma}) + \frac{M_{t+1,s}}{P_t} = \frac{Z_t A_{t,s}}{\gamma} + (1 + i_t^M) \frac{M_{t,s}}{P_t} + (W_{t,s} - T_{t,s})$$
(2)

Any interest on money holding i_t^M is assumed to be zero.

Maximising (1) subject to (2), defining $J(A_{t,s}, \frac{M_{t,s}}{P_t})$ as the value function of the dynamic-programming problem so

$$J(A_{t,s}, \frac{M_{t,s}}{P_t}) = \max\left[\frac{C_{t,s}^{1-\alpha}}{1-\alpha} + \frac{\phi}{1-\sigma}(\frac{M_{t,s}}{P_t})^{1-\sigma}\right] + \beta\gamma E_t J(A_{t+1,s}, \frac{M_{t+1,s}}{P_{t+1}})$$
(3)

Initially we will assume that return bearing assets are perfect substitutes so that we do not solve for ω . Hence, choosing $\{C_{t,s}\}_{t=s}^{t=\infty}$ and $\{\frac{M_{t,s}}{P_t}\}_{t=s}^{t=\infty}$, optimality requires satis faction of the Euler equations:

$$\Lambda_{t,t+1} = \beta \left(\frac{C_{t+1,s}}{C_{t,s}}\right)^{-\alpha} \tag{4}$$

this condition ensures that individuals allocate consumption optimally over time, bal-

ancing marginal utility across periods; and

$$\phi(\frac{M_{t,s}}{P_t})^{-\sigma}C_{t,s} = 1 - E_t(\frac{P_t}{P_{t+1}}\Lambda_{t,t+1}) = \frac{i_t^S}{1 + i_t^S}$$
(5)

which inverting, yields

$$\frac{M_{t,s}}{P_t} = \left[\phi C_{t,s} \frac{1 + i_t^S}{i_t}\right]^{\frac{1}{\sigma}} \tag{6}$$

so the demand for real money balances depends on consumption and the interest rate on bonds. Higher interest rates reduce the attractiveness of holding money.

Note, solving from the cohort budget constraint by forward substitution

$$\sum_{\tau=0}^{\infty} (\gamma)^{\tau} E_t(\Lambda_{t,t+\tau} C_{t+\tau,s}) = \sum_{\tau=0}^{\infty} \gamma^{\tau} E_t(\Lambda_{t,t+\tau} W_{t+\tau,s}) - \sum_{\tau=0}^{\infty} \gamma^{\tau} E_t(\Lambda_{t,t+\tau} T_{t+\tau,s}) + A_{t,s} + \frac{M_{t,s}}{P_t}$$
(7)

where

$$\Lambda_{t,t+\tau} = \prod_{j=0}^{j=\tau} \frac{1}{(1+r_{t+j})}$$

$$\lim_{T \to \infty} \Lambda_{t,t+T} A_{t+T,s} = 0$$
(8)

or

$$\sum_{\tau=0}^{\infty} (\beta \gamma)^{\tau} E_t(\Lambda_{t+\tau} C_{t+\tau,s}) = H_{t,s} - \overline{T}_{t,s} + A_{t,s} + \frac{M_{t,s}}{P_t}$$

$$(9)$$

So, the present value of consumption equals the present value of income minus taxes, plus initial wealth. Also, we have that human wealth, the present value of wages, and the present value of taxes, are given by respectively:

$$H_{t,s} = \sum_{\tau=0}^{\infty} \gamma^{\tau} E_t(\Lambda_{t,t+\tau} W_{t+\tau,s})$$
(10)

$$\overline{T}_{t,s} = \sum_{\tau=0}^{\infty} \gamma^{\tau} E_t(\Lambda_{t,t+\tau} T_{t+\tau,s})$$
(11)

and $A_{t,s} + \frac{M_{t,s}}{P_t}$ is initial wealth.

The consumption function for the cohort follows from (4) and (9):

$$C_{t,s} = \frac{H_{t,s} - \overline{T}_{t,s} + A_{t,s} + \frac{M_{t,s}}{P_t}}{\sum_{t=0}^{\infty} \gamma^{\frac{t}{\alpha}} [\beta(E_{z_t} Z_t)^{1-\alpha}]^{\frac{t}{\alpha}}}$$

To guarantee convergence of the forward iteration in the denominator, $\gamma(\beta(E_{z_t}Z_t)^{1-\alpha})^{\frac{1}{\alpha}} < 1$, so

$$C_{t,s} = \left\{1 - \left[\gamma \beta (E_{z_t} Z_t)^{1-\alpha}\right]^{\frac{1}{\alpha}}\right\} (H_{t,s} - \overline{T}_{t,s} + A_{t,s} + \frac{M_{t,s}}{P_t})$$
(12)

In this consumption function, the portfolio-return term takes expectations with respect to the probability distribution of z_t . The impact of the return term depends critically upon the value of α , turning on the critical value of $\alpha = 1$ or log utility. For $\alpha < 1$, the return derivative is negative and for $\alpha > 1$, the return derivative is positive.

³For more details on this derivation see Levhari and Mirman (1977).

We can now aggregate over cohorts. With a constant birth rate $\psi = (1 - \gamma) \ge 0$ and a survival rate $\gamma \ge 0$, total consumption is

$$C_t = (1 - \gamma) \sum_{s = -\infty}^{t} \gamma^{t-s} C_{t,s}$$

$$\tag{13}$$

Analogously

$$A_t = (1 - \gamma) \sum_{s = -\infty}^{t} \gamma^{t-s} A_{t,s}$$

$$\tag{14}$$

$$H_t = (1 - \gamma) \sum_{s = -\infty}^{t} \gamma^{t-s} H_{t,s}$$

$$\tag{15}$$

$$\overline{T}_t = (1 - \gamma) \sum_{s = -\infty}^t \gamma^{t - s} T_{t,s}$$
(16)

and finally, aggregate money demand is

$$\frac{M_t}{P_t} = (1 - \gamma) \sum_{s = -\infty}^{t} \gamma^{t - s} \frac{M_{t,s}}{P_t}$$

$$\tag{17}$$

2.2 Firms

When individuals are born, they begin work and so long as they survive they accumulate wealth by investing in the economy's competitively run technology. The dividends from the technology are paid to surviving individuals and to dying individuals as part of annuity payments. Firms are competitive and employ capital and labour to produce goods. The production function is Cobb-Douglas, $Y = F(K, L) = K^{\varepsilon}L^{1-\varepsilon}$. The profits of firms are paid as dividends to the owners of equities, who in this economy are mutual insurance companies. Hence, $\tilde{D}_t = \alpha \tilde{Y}_t - I_t - \Phi(I_t)$, where $I_t = K_t - (1 - \delta)K_{t-1}$ is investment and $\Phi(I_t)$ with $\Phi' > 0$ and $\Phi'' > 0$ are convex adjustment costs. The value of equities, the claim on the income from capital is

$$Q_t = D_t + \Lambda_{t+1} Q_{t+1} \tag{18}$$

Given

$$\lim_{T \to \infty} \Lambda_{t,t+T} Q_{t+T} = 0 \tag{19}$$

$$Q_t = \sum_{\tau=0}^{\infty} E_t(\Lambda_{t+\tau} D_{t+\tau})$$
 (20)

Firms invest to maximise the value of equity, so $Q'_t - 1 = \Phi'(I_t)$, which, if $\Phi(I_t) = \frac{1}{2\kappa}I_t^2$, yields:

$$I_t = \kappa(q_t - 1) \tag{21}$$

where
$$q_t = Q_t' = \sum_{\tau=0}^{\infty} E_t(\Lambda_{t+\tau} \varepsilon(\frac{K_{t+\tau}}{L_{t+\tau}})^{\varepsilon-1}).$$

2.3 Government

Having elaborated the households' and firms' optimisation problems, we now turn to the government's budget constraint. We first write down the uses and sources of funds identity in nominal terms for the central government (the treasury),

$$P_tG_t + i_t\widehat{B}_{t-1} \equiv P_tT_t + (\widehat{B}_t - \widehat{B}_{t-1}) + CBR_t$$

where G_t is government expenditure, T_t is taxes, \widehat{B}_t is the total value of outstanding government debt, CBR_t are receipts from the central bank, and i_t is the weighted average nominal interest rate. The monetary authority (central bank) uses and sources of funds condition is

$$(B_t^{CB} - B_{t-1}^{CB}) + CBR_t \equiv i_t B_{t-1}^{CB} + (\overline{M}_t - \overline{M}_{t-1})$$

where B_t^{CB} are government bonds held by the central bank and $\overline{M_t}$ is the outstanding stock of high-powered (base) money. Consolidating the two conditions, letting $B_t \equiv \hat{B}_t - B_t^{CB}$ be the nominal stock of government bond held by the public and expressing in real terms, we get

$$G_t + i_t \frac{B_{t-1}}{P_t} \equiv T_t + (\frac{B_t}{P_t} - \frac{B_{t-1}}{P_t}) + (\frac{\overline{M}_t}{P_t} - \frac{\overline{M}_{t-1}}{P_t})$$
 (22)

With different maturities of debt, the total real value of government debt, $\frac{B_t}{P_t}$, is comprised of short-term (one period) government bonds and long-term government bonds:

$$\frac{B_t}{P_t} \equiv \frac{B_t^S}{P_t} + \frac{B_t^L}{P_t} \tag{23}$$

Each period, some constant fraction, θ , of long-term bonds, B_t^L , mature, so conversely $(1-\theta)$ do not mature, and B_t^{LNew} new bonds are issued, $B_t^L = (1-\theta)B_{t-1}^{LOld} + B_t^{LNew}$. All short-term bonds are by definition, new. In turn

$$i_t^L B_t^L = (1 - \theta) i_t^L B_{t-1}^{LOld} + i_t^L B_t^{LNew}$$
 (24)

If $\eta = B_t^S/B_t$ is the fraction of debt that is short-term and the average maturity of long-term debt is $1/\theta$, then the average debt maturity is given by $\eta + (1 - \eta)(1/\theta)$.

The interest rates on the bonds satisfy the inter-temporal pricing conditions, respectively for short-term bonds

$$1 = E_t(\Lambda_{t+1} \frac{P_t}{P_{t+1}} (1 + i_t^S))$$
(25)

and for long-term bonds

$$1 = E_t(\Lambda_{t+1} \frac{P_t}{P_{t+1}} (1 + i_t^{LNew} + g_t))$$
 (26)

where $g_t = (B_t^{LOld} - B_{t-1}^{LOld})/B_{t-1}^{LOld}$ is the capital gain (loss) per period due to interest

rate movement. Also, we have the term-structure relationship:

$$(1 + i_t^{LNew}) = E_t \prod_{j=0}^{j=L} \Lambda_{t+j} (1 + i_{t+j}^S)^j$$
(27)

The government budget constraint is:

$$\frac{B_t^S + B_t^L}{P_t} + \frac{M_t}{P_t} = \frac{(1 + i_t^S)B_{t-1}^S + (1 + i_t^L)B_{t-1}^L}{P_t} + (1 + i_t^M)\frac{M_{t-1}}{P_t} + (\psi + \gamma)(T_{t+\tau} - G_{t+\tau})$$
(28)

with $B_t^L = (1 - \theta)B_{t-1}^{LOld} + B_t^{LNew}$. Clearly given $\psi = (1 - \gamma)$, $(\psi + \gamma) = 1$, reflecting the stable population with non-survivors being replaced by births. Using $1 = E_t(\Lambda_{t+1} \frac{P_t}{P_{t+1}}(1+i_t))$ and integrating the budget constraint gives

$$\frac{B_t^S + B_t^L}{P_t} + \frac{M_t}{P_t} = \frac{1}{(1+i_t)} \left[\sum_{\tau=0}^{\infty} E_t(\Lambda_{t,t+\tau}(s_{t+\tau}^f + s_{t+\tau}^s)) + \lim_{T \to \infty} E_t(\Lambda_{t,t+T}(s_{t+T}^f + s_{t+T}^s)) \right]$$
(29)

Here, $s_{t+\tau}^f = (T_{t+\tau} - G_{t+\tau})$; and $s_{t+\tau}^s = (i_{t+\tau}^S - i_{t+\tau}^M)(\overline{\frac{M_\tau}{P_\tau}})$ is seigniorage. The seiniorage term is revenue and hence a source of funds the government gets to use to purchase goods or save taxes, by being able to fund purchases through the monetary base, on which it pays a lower rate of interest, $0 \le i_t^M < i_t^S$. Here we assume that the interest rate on the monetary base i_t^M is zero. This means that if the government borrows from the central bank, its effective borrowing rate is zero so that monetary creation is a pure inflation tax at the rate of growth of the money supply denoted by μ .

Also, we have

$$\lim_{T \to \infty} E_t(\Lambda_{t,t+T}(s_{t+T}^f + s_{t+T}^s)) = 0$$
(30)

which is the transversality condition. Satisfaction of this condition is necessary for the forecast sequence of fiscal and seigniorage surpluses to be sustainable. This means that the debt-to-income ratio can be kept under control. If the transversality condition is satisfied for all policy sequences for positive prices, these policies are called Ricardian. If policy paths exist for which the transversality condition is not satisfied for all price paths, but only at equilibrium prices, these policies are called non-Ricardian. In the latter case, the government's budget condition is an equilibrium condition. At equilibrium prices, the transversality condition will be satisfied for both Ricardian and non-Ricardian government policies.⁴ In this model there is a real price level anchor, so the price level is determined by real portfolio choices and intergenerational wealth effects not just nominal government solvency.⁵

⁴The distinction between Ricardian and non-Ricardian policy regimes is made in Sargent and Wallace (1980). In the Ricardian regime, fiscal policy is passive, adjusting to ensure government solvency given monetary policy. Monetary policy is active, setting the nominal anchor. In the non-Ricardian regime, fiscal poicy is active, determining the path of primary surpluse and debt. Monetary policy is passive, adjusting monetary policy to support the fiscal constraint, through seigniorage or inflation.

⁵This non-Ricardian equilibrium is sometimes described as a "dividend equilibrium", where the government's liabilities are like equity claims on future surpluses. This mirrors how equity prices adjust to match expected future dividends in financial markets. See Norman and Wilem (2025). This mirrors Cochrane (2023) and his earlier work where he treats government debt as an equity-like claim on future primary surpluses, arguing that the price level adjusts to ensure the real value of debt equals the present

3 Market Equilibrium

If return bearing assets, equities and bonds, are perfect substitutes, there is only one market equilibrium condition for these assets. The aggregate market equilibrium condition for financial assets is

$$(1 - \gamma) \sum_{s = -\infty}^{t} (\gamma)^{t - s} A_{t, s} = Q_t + \frac{B_t}{P_t}$$
(31)

The left-hand-side of this equation is equal to the asset holding held by all of the surviving cohorts up until date t. Money is held by households and must equal the value of the money supply in equilibrium:

$$(1-\gamma) \sum_{s=-\infty}^{t} (\gamma)^{t-s} \left[\phi C_{t,s} \frac{1+i_t^S}{i_t^S}\right]^{\frac{1}{\sigma}} = \frac{\overline{M}}{P_t}$$
(32)

We also have the consolidated government budget condition:

$$\frac{B_t^S + B_t^L}{P_t} + \frac{\overline{M}_t}{P_t} = \frac{1}{(1+i_t)} \left[\sum_{\tau=0}^{\infty} E_t (\Lambda_{t,t+\tau}(s_{t+\tau}^f + s_{t+\tau}^s)) + \lim_{T \to \infty} E_t (\Lambda_{t,t+T}(s_{t+T}^f + s_{t+T}^s)) \right]$$
(33)

where the last term is zero if the transversality condition (30) is satisfied.

Equation (33) typically holds as an accounting identity, reflecting the ex post balance of government liabilities and revenues. That is, the consolidated government budget constraint, must hold ex post for any sequence of fiscal and monetary policies. However, when combined with a transversality condition on government debt, it becomes an equilibrium condition that determines the price level. This occurs in models where fiscal policy is active (i.e., primary surpluses are predetermined and not adjusted in response to debt dynamics) and monetary policy is passive (i.e., interest rates do not respond aggressively to inflation). In such regimes, the price level adjusts to ensure that the present value of government liabilities equals the present value of future fiscal surpluses and seigniorage. This mechanism underpins the Fiscal Theory of the Price Level (FTPL), as formalized in Woodford (1995, 2001) and Cochrane (2023). In contrast, under Ricardian regimes, fiscal policy adjusts to ensure solvency at any price level, and the budget constraint remains an identity. However, in certain policy regimes, it becomes an equilibrium condition that determines the price level. This will be true in our modelling.

Goods market equilibrium is given by:

$$C_t + I_t + \Phi(I_t) + G_t = Y_t \tag{34}$$

From (13), using (12), (14) and (16) we obtain:

$$C_{t} = \{1 - [\gamma \beta (E_{z_{t}} Z_{t})^{1-\alpha}]^{\frac{1}{\alpha}}\} [H_{t} - \overline{T}_{t} + A_{t} + \frac{M_{t}}{P_{t}}]$$

value of expected fiscal surpluses.

By substitution of (31) to eliminate A_t and consolidating income from labour (wages) and capital (dividends) into a single income term, Y_t ,

$$C_t = \left\{1 - \left[\gamma \beta (E_{z_t} Z_t)^{1-\alpha}\right]^{\frac{1}{\alpha}}\right\} \left[\sum_{\tau=0}^{\infty} \gamma^{\tau} E_t(\Lambda_{t+\tau}(Y_{t+\tau})) - \overline{T}_t + Q_t + \frac{B_t}{P_t} + \frac{\overline{M}}{P_t}\right]$$
(35)

Then letting $S_t = Y_t - C_t$, we can replace (34) with

$$S_t = I_t + \Phi(I_t) + G_t \tag{36}$$

which is the economy's IS curve.

The nominal rate of interest is a policy variable set by a target rule (a Taylor rule). According to Taylor's original version of the rule, the nominal interest rate should respond to divergences of actual inflation rates from target inflation rates and of actual Gross Domestic Product (GDP) from potential GDP:

$$i_t^S = \pi_t^* + r_t^* + a_\pi (\pi_t - \pi^*) + a_y (Y_t - \overline{Y})$$
(37)

where a_{π} and a_{y} are policy weights. Here, however, we are assuming fully flexible prices and no output gap, $Y_{t} = \overline{Y}$. Moreover, we assume that $a_{\pi} > 1$.

In this economy, the real rate of interest is set to satisfy (36). The short-term nominal rate of interest is a policy variable set to achieve the inflation objective set by (37). This means that the money market equilibrium condition (32) takes this rate as given so that it solves for the quantity of money. Assuming that the all of the right-hand side variables in the condition (33) are exogenously set policy variables, if the transversality condition (30) is satisfied, the consolidated government budget condition (33) is an equilibrium condition that determines the price level.⁶

4 Policy

This section explores how fiscal and monetary interventions affect real outcomes through redistribution, even in the absence of nominal frictions. We focus on three key channels: debt-financed tax cuts, changes in the maturity structure of government debt, and adjustments to the inflation target. Each policy alters household budget sets and intertemporal resource allocation, generating real effects via consumption, savings, and investment decisions.

4.1 Debt Financed Tax Cuts and Ricardian Equivalence

In a frictionless economy with infinite horizons, Ricardian equivalence suggests that debt-financed tax cuts should be neutral: households internalize future tax liabilities

⁶The model treats money as non-causal but necessary. It is not a source of nominal determinacy; rather, the price level is determined by fiscal solvency via the intertemporal budget constraint. With the nominal interest rate set by policy and the price level pinned down by the fiscal side, the money stock adjusts residually to satisfy money market equilibrium. If the Taylor rule were dropped, the interest rate would be determined by liquidity preference, potentially introducing indeterminacy.

and adjust savings accordingly. However, in our model, finite life expectancy and a positive birth rate break this neutrality. Future tax liabilities are partially borne by unborn cohorts, creating a net wealth effect for current households. As a result, debt-financed tax cuts increase current consumption, reduce savings, and raise the real interest rate. Investment falls, and the capital stock declines. The present value of government surpluses shrinks, necessitating a higher price level to satisfy the intertemporal budget constraint. This leads to a reduction in real money balances and an increase in the nominal interest rate. The policy redistributes resources from future to current taxpayers, generating real effects even in a frictionless setting.

To see this formally. In our model, from the government budget condition (33), with the birth rate equal to the death rate but keeping terms for comparison purposes:

$$\Delta T_t + \sum_{\tau=0}^{\infty} E_t \Lambda_{t,t+\tau} (\psi + \gamma)^{\tau} \Delta T_{\tau+\tau} = 0$$
(38)

with $\psi = 1 - \gamma$. For households alive at date t, using the lifetime budget constraint, the impact is

$$\Delta T_t + \sum_{\tau=0}^{\infty} E_t \Lambda_{t,t+\tau}(\gamma)^{\tau} \Delta T'_{t+\tau} > 0$$
 (39)

The reason the two effects are different is that the future tax liabilities are shared with yet unborn tax payers, $\psi > 0$, so for all τ , $\Delta T'_{t+\tau} < \Delta T_{\tau+\tau}$. If there is no birth, $\psi = 0$, $\Delta T'_{t+\tau} = \Delta T_{\tau+\tau}$, then the net wealth effect on consumers is zero. In the model, however, the assumption of a zero-death rate and no birth to keep the population constant delivers neutrality, however, this is an artifact of the model assumption, $\psi = 1 - \gamma$. The crucial element for non-neutrality is a positive birth rate. The unborn are not part of the surviving population's decision problem but will pay some future taxes. So as there is birth in the model, $(1-\gamma) > 0$, we have non-neutrality and more so if future tax increases are further into the future. That is, the debt payment impact falls disproportionately on yet unborn generations. The positive wealth effect in turn implies that $-\Delta T_t + \frac{\Delta B_t}{P_t} <$ 0. This means that consumers at date t increase consumption, so that saving must increase by less than the tax cut. Hence savings must increase by less than the value of government bonds issued to finance the tax cut. But if savings increase by less than the value of the tax cut, the real rate of interest will increase and investment and the capital stock will be lower. At the same time, the present value of government surpluses will be lower, and given the sequence of fiscal surpluses and seiniorage revenues, this necessitates an increase in the price level. Note also that this implies an decrease in the value of real money balances, thereby necessitating an increase in the nominal rate of interest. At a constant inflation rate this is consistent with a higher real interest rate and in turn a lower level of financial wealth.

Empirical evidence supports the model's prediction that Ricardian equivalence breaks down in the presence of finite horizons and demographic turnover. Cadsby and Frank (1991) conducted experimental tests using overlapping generations and found that Ricardian neutrality holds only under specific conditions, such as positive bequests. When

⁷This point is emphasised in Buiter (1988).

these are absent or constrained, households exhibit Keynesian behavior, increasing consumption in response to tax cuts. Their design mimics finite horizons and demographic turnover, validating our assumption that Ricardian equivalence fails under these conditions.

4.2 Debt Maturity and Intertemporal Redistribution

The maturity structure of public debt influences the timing of tax liabilities and the distribution of wealth across cohorts. Substituting long-term debt for short-term debt defers tax payments, shifting the burden to future generations. If households view different maturities as imperfect substitutes—due to liquidity preferences or rollover risk—then changes in debt composition affect consumption and savings behavior. In our model, lengthening debt maturity increases the net wealth of current consumers, raising their consumption and reducing savings. This mirrors the non-neutrality observed in the Ricardian case, but arises from the timing of payments rather than the total tax burden. The policy redistributes intertemporally, benefiting current cohorts at the expense of future ones.

Barro (1979) started a literature examining the role of the maturity structure of government debt as one of inter-temporal tax smoothing. This sees the fundamental problem as one of meeting the government's commitments but at the same time setting taxes to minimise distortions. However, in the current context we assume lump sum taxes. The approach taken here is to consider debt policy as one of smoothing shocks through a dynamic insurance mechanism. The model provides a simple way to see the implications of the maturity structure of the public debt. In the model we present, any non-neutrality of government debt policy will emerge from the composition of government debt impacting the budget sets of households and thereby their consumptionsavings decisions. The problem here is seen as a Modigliani-Miller problem, along the lines of Wallace (1981) and Chamley and Polemarchakis (1984). Wallace looked at the impact of changes in the composition of the government's (inclusive of the central bank) balance sheet on household budget sets and market equilibrium conditions. The analysis he conducts is similar to the general equilibrium analysis of corporate financial policy undertaken by Stiglitz (1969). Consider an initial equilibrium with a particular composition of government debt held by households to provide a particular profile of payment to them. At this equilibrium, household budget sets, asset holdings and consumption demands are given. Equilibrium determines equilibrium market returns on stock and bonds and the value of money holdings. Implied annuity transfers are also determined. Suppose that at this equilibrium, debt maturity is changed by substituting one maturity for another, so say average maturity is increased by substituting longer-term debt for short-term debt. This will be irrelevant if households view the new maturity structure as a perfect substitute for the initial structure, with no impact of the change on the distribution of tax liabilities needed to finance the total payments on the debt.

Let us suppose that initially all of the debt is short term. Then the government debt is a sequence of short-term government bonds that must be rolled over to equal the present value of primary surpluses and seigniorage payments. This implies a sequence of tax payments and hence $\{s_{\tau}^f\}_{\tau=t}^{\tau=\infty}$ satisfying equation (33). We need to understand the impact of debt policy. The initial equilibrium with the government rolling over short-term bonds translates into the composition of the sequence of household budget sets and consumption decisions. In equilibrium there is a path of discount factors $\{\Lambda_{t+\tau}\}_{\tau=0}^{\tau=\infty}$, price levels $\{P_{t+\tau}\}_{\tau=0}^{\tau=\infty}$ and hence implied interest rates satisfying (25) and (26).

Now consider a policy of substituting long-term debt for short-term debt, with $\Delta \frac{B_t^S}{P_t} + \Delta \frac{B_t^L}{P_t} = 0$. This impacts the left-hand-side of (33) through a change in debt composition only. This change in the composition of the debt will not impact the tax financed payments on the total amount of debt if a sequence of rolled over short-term debt is a perfect substitute for long-term debt, so that any long-term bond can be costlessly decomposed into a sequence of short term bonds. Then issuing long-term bonds will be equivalent in expected value to the sequence of rolled over short-term bonds they replace in household portfolios, provided the real (inflation adjusted) sequence of payments to the bond-holders is the same. If long-term bonds can be used to satisfy tax liabilities without any additional cost, the maturity substitution will be neutral in its effects.

On the other hand, if the substitution of longer-term for short-term debt changes the profile of tax liabilities by pushing these payments further into the future, then on the right-hand-side of (33), the pattern of primary surpluses must change. The payments to bond-holders in the immediate term must be reduced and longer-term payments must be increased. This is neutral from the stand-point of the government's budget constraint. This in turn means that the price level does not change. However, it reduces tax payments in the short-term and increases them in the longer-term. These later payments are a transfer of tax burden in part to future, yet unborn, tax-payers. Hence, the net wealth of current consumers is increased and so is their consumption. The non-neutrality and real impact is therefore of a similar nature to the case of non-Ricardian equivalence discussed above.

Experimental evidence from March and von Weizsäcker (2020) demonstrates that older generations strategically coordinate bond holdings to influence intergenerational redistribution. Their lab-based implementation of Tabellini's model (1991) shows that debt maturity affects the timing and burden of tax liabilities, consistent with our model's prediction that longer maturities shift burdens to future cohorts and increase current consumption. This supports the view that debt composition is not neutral and has real redistributive effects.⁸

4.3 Inflation Targeting and the Tobin-Mundell Effect

In our model, adjusting the inflation target affects portfolio allocation through a Tobin-Mundell channel. A higher inflation target raises nominal interest rates, reducing real money balances and prompting households to shift toward interest-bearing assets. This

⁸Taballini (1991) develops a political-economic model of public debt in an overlapping generations framework, showing how current generations can use debt to redistribute resources in their favor, and how political coordination affects debt repayment. It's foundational for understanding strategic intergenerational redistribution.

increases demand for capital, lowers real interest rates, and stimulates investment. In the infinite-horizon case with separable utility, monetary growth is super-neutral: it does not affect real variables. However, with finite lives and a positive birth rate, monetary growth raises seigniorage revenues, reduces lump-sum taxes, and increases human wealth. The resulting fall in the real interest rate boosts capital accumulation and output. The redistributive effect favors borrowers over savers, altering consumption and investment patterns. We now examine these findings in detail.

Mundell (1965) and Tobin (1965) considered the impact on investment and capital holding through a portfolio balance effect. Now consider the impact of a change in the inflation target. In this model consider an increase in π^* in the Taylor rule (37). This must be accommodated by an increase in monetary growth. This in turn raises the nominal interest rate, which in (32) reduces the demand for money and so to maintain the inflation target the stock of money must be reduced. The reduction in money holding causes a substitution towards interest bearing assets. This will be enhanced by a negative impact on the value of outstanding government bonds. Given the stock of government bonds in the model, this necessitates an increase in holdings of equity in real capital. This must reduce real interest rates, which increases Q and so investment and capital accumulation. At the same time if $\alpha > 1$, so that the impact of lower returns on consumption in (35) is negative, so saving increases. In equilibrium, the difference between the real and nominal interest rates satisfies the Fisher equation and so at lower real rates the change in the nominal rate of interest will be less than the change in the inflation target.

Of course, the above reasoning has to be modified in our model. Our model has money in the utility function as in Sidrauski (1967). In the pure infinite horizon case with an infinite horizon, which obtains with a zero-birth rate (and no death), superneutrality obtains, so the steady state real interest rate and capital stock is independent of the inflation rate. Consider the special case of a zero birth and death rate, $\gamma = 1$. In that case the real interest rate must equal the rate of time preference, $r = \rho$, and therefore the capital stock is independent of the monetary growth rate. Moreover, consumption is unaffected. An increase in monetary growth, μ , increases the nominal interest rate one-for-one and therefore reduces holdings of real money balances. It can be shown that real seignorage revenues, $\mu_{P_t}^{M_t}$, increase, so that lump-sum taxes fall and human wealth increases. Moreover, the fall in non-human wealth, caused by the reduction in real money balances, is exactly off set by the increase in human wealth, so that total wealth and the consumption of physical goods are unaffected. Marini and Van der Ploeg (1988) show that when $\gamma = 1$, so lives are infinite, and the sub-utility function is weakly separable in consumption and real balances, as in our model, the real part of the dynamic system separates out from the monetary part and therefore monetary growth does not affect the transitional dynamics of the real variables. However, when the sub-utility function is not weakly separable, monetary growth affects the marginal propensity to consume goods out of total wealth and thus affects the dynamics, but it does not affect the steady-state value of capital (see Fischer, 1979).

Now consider the general case of finite lives, $\gamma < 1$ and a positive birth rate. Now changes in monetary growth affect the steady-state value of the capital stock. Even a weakly separable sub-utility function generates this non-neutrality result. With finite lives and positive birth and death rates an increase in monetary growth leads in the long run to an equal increase in inflation, a fall in the real interest rate, an increase in capital, output, and consumption. In this model there is also a fall in the level of real money balances. Of course, as Marini and van der Ploeg (1988) point out, this effect is very similar to the conventional Mundell-Tobin effect. This non-neutrality arises, because with finite lives a wedge is driven between the discount rate used to calculate the value of government surpluses, which in the absence of risk and $\psi + \gamma = 1$ is r, and the one used to calculate human wealth, $r+(1-\gamma)$. This can be seen in the algebra of the model along similar lines as in the case of Ricardian equivalence examined above. Monetary growth raises seigniorage revenues (despite a fall in real money balances) and therefore reduces lump-sum taxes. Households human wealth increases because lump-sum taxes fall. This impact is enhanced by an increase in wages and a fall in the real rate of interest.

Edwards (2006) provides empirical support for the Tobin-Mundell effect in low-inflation environments. Using a panel of countries with inflation rates between 5–9%, he finds a statistically significant positive correlation between inflation and investment. His analysis controls for political and institutional factors and confirms that moderate inflation can stimulate capital accumulation. This aligns with our model's prediction that higher inflation targets reallocate portfolios toward productive assets and increase investment.

5 Extending the Model

To deepen our understanding of redistribution and policy impacts, we now extend the model to incorporate agent heterogeneity. Specifically, we introduce two types of individuals born at each date who differ in their time preferences, This heterogeneity introduces borrowing and lending behavior, default risk, and insurance mechanisms that amplify the redistributive effects of fiscal and monetary policy. Agent heterogeneity is introduced along the lines examined extensively by Farmer (see for example Farmer (2016)). The simple extension is to have two types of individual born at each date who differ purely in terms of their time preference. There is a high time preference group 1, with time preference factor β_1 , who want to consume more earlier and indeed may want to borrow in the early phase of life. There is a second group with lower time preference, $\beta_2 > \beta_1$, who never borrow and can act as lenders to borrowers.

5.1 Borrowing, Lending, and Default Risk

In our model, impatient agents (group 1) prefer early consumption and may borrow against future income. Patient agents (group 2) act as lenders. Borrowing takes the form of consumption loans, which are repaid later in life or covered by life insurance in

the event of premature death. Insurance companies pool risk and charge actuarially fair premiums, ensuring that lenders are repaid regardless of borrower mortality. This structure introduces a wedge between borrowing and lending rates, reflecting default risk and insurance premia. It also creates asymmetries in consumption opportunities: borrowers face liquidity constraints and depend on future income, while lenders accumulate wealth and annuities over time.

We note that in our general framework, borrowing could take the form of short sales of return bearing assets, combined with life insurance. Here the borrower, borrows a portfolio of assets which are then sold. The borrower then uses the proceeds to finance consumption but will have to ensure that they have saved enough later to repurchase the assets and settle the short position. However, if they die before the account is settled, at least in part, the lender is exposed to either a full or partial default. This could be handled by changing the nature of annuities contracts in a complex way. An alternative is pure consumption loans. The lender will offer consumption loans to the impatient borrower. The loans are held in lenders portfolios along-side government bonds and equities and are used by borrowers to fund consumption. To ensure that in the event of death the loan can be repaid and offer a return equivalent to long positions in assets combined with equities, the loans must be insured by short-positions in annuities backed by long-positions in return bearing assets or command higher rates with a significant default risk premium paid in solvent states.

Let us suppose that borrowing takes place, borrowers plan to repay loans later but in the event that they die their debts are paid by life insurance. The lender will be paid for sure either from the surviving borrower or from a insurance company. The insurance company collects insurance risk premia from borrowers, pooling loans across borrowers and setting premia on competitive fair terms. We assume that insurance companies are endowed with capital from history so that they can meet debts of borrowers who die in debt.

We assume that the proportion of type β_1 born at each date is $0 < \lambda < 1$. The consumption-savings decisions of the two groups are technically the same as above, the principal difference is that there are two groups differing by discount rate and the recognition that net borrowers have no assets to transfer in the event of their death, rather debts that must be covered by life-insurance. We do not examine the dynamic programming problem in any detail.⁹ For each group, the consumption functions are the same linear functions as in (13). For the high-time preference group, let the flow

⁹The household's dynamic programme is treated as smooth in the sense that there are no non-convexities between phases of the household's life cycle, such as switching between borrowing and lending. Hence in the case of a hard no borrowing constraint binding, we will treat it as fixed. In a more general framework we would need to consider left and right derivatives of the value function with respect to the state variable $A_{t,s}$ at points of phase transition and discontinuity in the consumption control variable, $C_{t,s}$.

budget constraint be written as

$$C_{t,s}^{1} + \gamma E_{t} \left(\Lambda_{t,t+1} \frac{Z_{t+1} A_{t+1,s}^{1}}{\gamma}\right) + \gamma \frac{M_{t+1,s}^{1}}{P_{t}} - \gamma E_{t} \left(\Lambda_{t,t+1} \frac{(1+i_{t}^{S})}{\gamma} L_{t+1,s}^{+}\right)$$

$$-\gamma V_{t,s}^{*} = \frac{Z_{t} A_{t,s}^{1}}{\gamma} + L_{t,s}^{+} + (1+i_{t}^{M}) \frac{M_{t,s}^{1}}{P_{t}} + (W_{t,s} - T_{t,s})$$

$$(40)$$

In the uses of funds on the left hand side of the expression along-side the loan repayment term is the premium, $V_{t,s}^*$, paid to the insurance company to cover the solvency risk of loans. In the borrowing phase, $A_{t,s}^1=0$ and and borrowing $L_{t,s}^{1+}>0$ in this phase. From the lenders perspective they are not exposed to solvency risk on these loans, so they attract the same interest rate as the short-term borrowing rate. For the β_1 group the consumption function is

$$C_{t,s}^{1} = \{1 - [\gamma \beta (E_{z_{t}} Z_{t})^{1-\alpha}]^{\frac{1}{\alpha}}\} (H_{t,s}^{1} - \overline{T}_{t,s} - \overline{V}_{t,s}^{*} + A_{t,s}^{1} + \frac{M_{t,s}^{1}}{P_{t}})$$
(41)

where $\overline{V}_{t,s}^*$ is the capital value of the insurance premiums.

For the β_2 group, who do borrow but lend and are on the opposite side of the competitively priced consumption loans, $L_{t+1,s}^+$, the flow budget constraint is

$$C_{t,s}^{2} + \gamma E_{t}(\Lambda_{t,t+1} \frac{Z_{t+1} A_{t+1,s}^{2}}{\gamma}) + \gamma \frac{M_{t+1,s}^{2}}{P_{t}} + \gamma E_{t}(\Lambda_{t,t+1} \frac{(1+i_{t}^{S})}{\gamma} L_{t+1,s}^{+})$$

$$= \frac{Z_{t} A_{t,s}^{1}}{\gamma} - L_{t,s}^{+} + (1+i_{t}^{M}) \frac{M_{t,s}^{1}}{P_{t}} + (W_{t,s} - T_{t,s})$$

$$(42)$$

The cohort's consumption function is

$$C_{t,s}^{2} = \left\{1 - \left[\gamma \beta (E_{z_{t}} Z_{t})^{1-\alpha}\right]^{\frac{1}{\alpha}}\right\} (H_{t,s}^{2} - \overline{T}_{t,s} + A_{t,s}^{2} + \frac{M_{t,s}^{2}}{P_{t}})$$
(43)

The aggregate consumption function is

$$C_{t} = \lambda \left[(1 - \gamma) \sum_{s = -\infty}^{t} \gamma^{t - s} C_{t, s}^{1} \right] + (1 - \lambda) \left[(1 - \gamma) \sum_{s = -\infty}^{t} \gamma^{t - s} C_{t, s}^{2} \right]$$
(44)

This aggregate function replaces (35) in the equilibrium condition (34).

The net aggregate return bearing asset holding is

$$\lambda \left[(1 - \gamma) \sum_{s = -\infty}^{t} (\gamma)^{t-s} A_{t,s}^{1} \right]$$

$$+ (1 - \lambda) (1 - \gamma) \sum_{s = -\infty}^{t} (\gamma)^{t-s} A_{t,s}^{2}$$

$$(45)$$

If return bearing assets are perfect substitutes, this quantity replaces the term on the left-hand-side of (31).

5.2 Credit Constraints and Consumption Dynamics

Some cohorts of impatient agents may be credit constrained, unable to borrow against future income. For these agents, current consumption is tightly linked to current income and taxes. A tax cut, therefore, leads to an immediate increase in consumption, amplifying the redistributive impact of fiscal policy. The presence of credit constraints modifies the aggregate consumption function and asset demand. It also affects the transmission of policy shocks, as constrained agents respond more strongly to changes in taxes, transfers, and interest rates.

To see this consider the case when it is not possible to borrow to access human capital to enhance current consumption as is assumed above. That is, individuals cannot short-sell interest bearing assets or buy life-insurance with borrowed funds. However, if there is a binding borrowing constraint for the β_1 group, consumption in the first phase of life involves:

$$C_{t,s}^{1} = \frac{Z_{t}A_{t,s}}{\gamma} + (1 + i_{t}^{M})\frac{M_{t,s}^{1}}{P_{t}} + (W_{t,s} - T_{t,s})$$
(46)

This means that any increase in $W_{t,s}$ or reduction in $T_{t,s}$ for this group will result in a one for one increase in consumption, $C_{t,s}^{1i}$.

Suppose that at time t, of the high-discount group β_1 , a particular cohort born at date s is constrained. This is indicated by the zero-one indicator variable $\sigma_{t,s}$ being equal to one. Then, the net demand for return bearing assets in (31) becomes

$$\lambda (1 - \gamma) \sum_{s = -\infty}^{t} (\gamma)^{t - s} A_{t,s}^{1} + (1 - \lambda)(1 - \gamma) \sum_{s = -\infty}^{t} (\gamma)^{t - s} (1 - \sigma_{t,s}) A_{t,s}^{2}$$
(47)

Given the simple modification of the model to include heterogeneity within cohorts, we reconsider the two simple exercises undertaken above.

5.2.1 Redistributive Effects of Fiscal Policy

We revisit the Ricardian equivalence result in the context of agent heterogeneity. The intertemporal budget constraint of the government remains unchanged, but the distributional impact of tax changes varies across types: Unconstrained impatient agents benefit from tax cuts due to intergenerational redistribution. Constrained impatient agents experience a direct increase in consumption, as they cannot smooth consumption over time. Patient agents adjust savings and consumption based on expected future taxes, with smaller immediate effects. The aggregate consumption response is a weighted sum of these effects, highlighting the importance of cohort structure and borrowing constraints in shaping fiscal policy outcomes.

We now show this formally. The changes to the model do not fundamentally change the governments inter-temporal budget condition. From the government budget condition, with the birth rate equal to the death rate

$$\Delta T_t + \sum_{\tau=0}^{\infty} E_t \Lambda_{t,t+\tau} (\psi + \gamma)^{\tau} \Delta T_{\tau+\tau} = 0$$
(48)

For households alive at date t, the combined impact on net wealth of the tax change is

$$\lambda \left[\Delta T_t + \sum_{\tau=0}^{\infty} E_t \Lambda_{t,t+\tau}(\gamma)^{\tau} (1 - \sigma_{t,s}) \Delta T'_{t+\tau}\right] + (1 - \lambda) \left[\Delta T_t + \sum_{\tau=0}^{\infty} E_t \Lambda_{t,t+\tau}(\gamma)^{\tau} \Delta T'_{t+\tau}\right]$$
(49)

where the terms $\sigma_{t,s} = 1$ for some s indicates that some β_1 group cohorts may be credit constrained and not able to access future wages and so do not discount the tax liability. This becomes material through the total impact on consumption:

$$\Delta C_{t} = \lambda \left[(1 - \gamma) \sum_{s=-\infty}^{t} \gamma^{t-s} \left\{ 1 - \left[\gamma \beta_{1} (E_{z_{t}} Z_{t})^{1-\alpha} \right]^{\frac{1}{\alpha}} \right\} \right]$$

$$\left[\Delta T_{t} + \sum_{\tau=0}^{\infty} E_{t} \Lambda_{t,t+\tau} (\gamma)^{\tau} (1 - \sigma_{t,s}) (\Delta T'_{t+\tau} + \Delta \overline{V}_{t,s}^{*}) \right]$$

$$+ \lambda \left[\sum_{s=-\infty}^{t} \sigma_{t,s} (\Delta T'_{t} + \Delta \overline{V}_{t}^{*}) \right] + (1 - \lambda) \left[(1 - \gamma) \sum_{s=-\infty}^{t} \gamma^{t-s} \left\{ 1 - \left[\gamma \beta_{2} (E_{z_{t}} Z_{t})^{1-\alpha} \right]^{\frac{1}{\alpha}} \right\} \right]$$

$$\left(\Delta T_{t} + \sum_{\tau=0}^{\infty} E_{t} \Lambda_{t,t+\tau} (\gamma)^{\tau} \Delta T'_{t+\tau} \right)$$

$$(\Delta T_{t} + \sum_{\tau=0}^{\infty} E_{t} \Lambda_{t,t+\tau} (\gamma)^{\tau} \Delta T'_{t+\tau})$$

$$(\Delta T_{t} + \sum_{\tau=0}^{\infty} E_{t} \Lambda_{t,t+\tau} (\gamma)^{\tau} \Delta T'_{t+\tau})$$

This ΔC_t term is made up of three big terms. The first term is the impact on the unconstrained cohorts of the β_1 group; and the second the impact on the constrained cohorts of this group; whilst the last term is the impact on the unconstrained β_2 group. All three of the consumption changes are positive. The first and third, because some of the future tax liabilities are borne by unborn households. The presence of the term $\psi > 0$ in (48) means that $\Delta T'_{t+\tau} < \Delta T_{\tau+\tau}$ for all cohorts and for all τ . Note, however, that all members of the β_1 group who borrow will benefit additionally from the tax cut by effectively borrowing at the government borrowing rate and save paying insurance premia, $\Delta \overline{V}_t^* < 0$, on these loans as the loans are financed through future lump-sum taxes. There is also a more significant effect from the presence of the credit constrained members of the β_1 group, who will pay future taxes but as they are constrained, spend the tax cut. Again, the impacts on the β_2 will be zero if $\psi = 0$, as $\Delta T'_{t+\tau} = \Delta T_{\tau+\tau}$. However, borrowing cohorts and in particular constrained cohorts will still see a positive impact on net wealth and consumption from effectively improved borrowing terms even when $\psi = 0$.

Isiaka, Mihailov, and Razzu (2024) offer empirical evidence that fiscal shocks have dynamic redistributive effects across income groups and countries. Their GMM Panel VAR analysis of 99 countries (2004–2014) reveals that education and health spending reduce inequality over time, particularly in middle- and high-income countries. This supports our model's emphasis on cohort-specific responses to tax changes and the importance of fiscal composition in shaping redistributive outcomes.

5.2.2 Debt Maturity and Clientele Effects

Debt maturity now interacts with agent heterogeneity. Impatient agents prefer shortterm instruments that align with their consumption profile, while patient agents favour long-term assets. This segmentation creates clienteles for different maturities, allowing the government to tailor its debt issuance to market demand. Changes in debt composition are seen to affect consumption opportunities asymmetrically. For example, lengthening debt maturity may benefit patient agents by increasing future payouts, while reducing liquidity for impatient agents. These effects introduce new channels for redistribution and raise questions about optimal debt design. We illustrate this argument in detail below.

In the extended model the issue of debt maturity is more complex. The debt market can be divided into clienteles who have different preferences for longer and shorter-term funding. This raises the potential for the government to cater to the demands of the market. Additional non-neutralities arise if different groups consumption opportunities are affected asymmetrically by changes in the government's debt policy. Here we consider segmenting the market for bonds, so that the bond portfolio required to finance the consumption for the β_1 group may differ from that for the β_2 group but for the moment assume that no households are credit constrained, $\sigma_{t,s} = 0$ for all s.

We assume short-term bonds are held between the β_1 group and the β_2 group with $\eta^{S1} + \eta^{S2} = 1$, where η^{S1} is the proportion of short-term bonds held by group 1; and similarly for long-term bonds $\eta^{L1} + \eta^{L2} = 1$. Q_t^1 is the equity holding of the β_1 group. The return bearing asset holdings of the β_1 , impatient group, is equal to the supply

$$\lambda (1 - \gamma) \sum_{s = -\infty}^{t} (\gamma)^{t - s} A_{t, s}^{1} = Q_{t}^{1} + \eta^{S1} \frac{B_{t}^{S}}{P_{t}} + \eta^{L1} \frac{B_{t}^{L}}{P_{t}}$$

$$(51)$$

They wish to consume relatively more now and less later in life but will need to build up assets later to ensure that they are solvent in the limit. The demand for return bearing assets and annuity contracts by cohorts on the left-hand-side of this expression imply a certain stream of payments to survivors. Older types must have relatively lower payments as they have consumed more earlier, this is the so-called humped savings hypothesis. This means that the portfolio of assets will need to deliver more income in the immediate future to match liabilities

Next consider the β_2 , more patient group:

$$(1 - \lambda)(1 - \gamma) \sum_{s = -\infty}^{t} (\gamma)^{t - s} A_{t,s}^2 = Q_t^2 + \eta^{S2} \frac{B_t^S}{P_t} + \eta^{L2} \frac{B_t^L}{P_t}$$
 (52)

At date t, this group of survivors from previous cohorts and the cohort born at date t will consume less than the β_1 group with a preference for later consumption, so that they hold more assets and more annuities. This group will save more and hold more assets and annuity contracts and thereby allocate more of their human capital to more distant consumption.

The question arises as to whether the government can cater to this (and so reduce its own funding costs) by issuing longer-term bonds that substitute for rolling-over short-term bonds, which will raise welfare only if it overcomes a constraint. Rolling over short-term bonds or indeed liquidating long-term bonds are equivalent if there is no roll-over risk or early-liquidation risk.

6 Further Extension of the Model

In this section, we extend the model to examine how the government can use the maturity structure of public debt to insure against two types of shocks: (1) fiscal shocks that affect government expenditure, and (2) income shocks that affect household budgets. These extensions highlight the role of debt design in smoothing intertemporal burdens and redistributing risk across cohorts.

In the analysis conducted so far, all that matters is distribution of tax liabilities. It is this that determines payments to debt, which could be perpetuities The retirement of bonds at some point will limit the burden of any taxes implied by debt falling on future generations. The same outcome can be achieved by rolling over short-term debt. Of course, this result is due to perfect substituted between maturities and in particular, the absence of liquidation risk for long-term bonds or roll-over risk for short-term bonds.

6.1 Fiscal Shocks and Government Budget Insurance

Suppose the government faces stochastic shocks to its expenditure path—such as war, recession, or natural disaster. In the absence of complete markets, the government cannot issue Arrow-Debreu securities to hedge these shocks directly. Instead, it must rely on the composition of its debt portfolio. Following Angeletos (2002), we show that issuing long-term debt (e.g. perpetuities) allows the government to smooth tax liabilities over time. By holding reserves in long-term bonds and adjusting the maturity profile of new issuance, the government can hedge against interest rate volatility and avoid sudden increases in tax rates. The key insight is that longer maturities reduce rollover risk and allow the government to defer payments, effectively insuring against short-term fiscal shocks. This strategy is optimal when the cost of refinancing short-term debt exceeds the liquidity risk of liquidating long-term bonds.

Let us first consider the illustrative example of a shock to the government's budget and ask how the government may meet shocks in a way that smooths or insures the impact. The optimal way of meeting the contingent needs is to be able to cover the income losses through a holding of (Arrow-Debreu) state-contingent claims. Angeletos (2002) provides a general framework in which the maturity structure of public debt provides the opportunity for the government to construct dynamic insurance against shocks. He shows that to span the state-space, the economy needs as many linearly independent income streams as states of the world at each date and the rebalancing of the portfolio at each date. To achieve this with different maturities is only be possible if the different maturities are not co-linear. In his framework the government uses debt policy as part of an optimal policy of funding (random) government expenditures with Ramsey taxation, when also faced with income and interest rate shocks. The

¹⁰Bohn (1990) analyses the optimal structure of government debt in a stochastic environment. He shows in a model with distortionary taxes, the government should smooth tax rates over states of nature as well as over time. Government liabilities should be structured to hedge against macroeconomic shocks that affect the government budget. The optimal structure of government liabilities generally includes some" risky" securities which are state-contingent in real terms.

optimal maturity structure of government debt provides perfect insurance and allows the government to sustain an invariant rate of taxation. Holding long-term debt and investing in a short-term asset can hedge the budget against both random variation in government expenditure and aggregate income, as well as against the risk of refinancing the outstanding debt at variable interest rates. However, it is still optimal to transform the initial debt to a perpetuity, so as to insulate the budget from the risk of refinancing public debt at variable interest rates.

Consider the government's budget condition (33) where the left-hand side is the value of the government's liabilities and the right-hand side is the value of its assets, the present value of fiscal surpluses. The right-hand-side may be subject to shocks. Assume that there is the possibility of a negative shock at each date to fiscal surpluses because of a jump in government expenditure, that is with probability v^f the current fiscal surplus falls by $\Delta^f s_t^f$ because of an increase in government expenditure and in the event of such a change assume by condition (37) that the short-term rate of interest jumps up by $\Delta^i i_t^S$, the possibility of these jumps is reflected in the term-structure and bond prices.

Following Angeletos (2002), suppose that the government structures its liabilities by making all long-term bonds perpetuities but also issuing some bonds to finance a reserve fund, R_t . The value of government bonds pre the fiscal shock and contributions to the reserve fund is $\frac{B_{t-1}}{P_t}$. Post the fiscal shock and contributions to the reserve fund, the value of the debt is $\frac{B_t}{P_t}$. The change in the value of bonds $\frac{B_t}{P_t}$ due to the interest rate change is $\Delta^i \frac{B_t}{P_t}$. The right-hand-side of (33) is the present value of fiscal surpluses, written as $PV(s_t^f)$. The difference in the value of $PV(s_t^f)$ due to the interest rate change is $\Delta^f PV(s_t^f)$. The profile of payments on the perpetuities is such that $\frac{B_t}{P_t} = PV(s_t^f)$ and $\Delta^i(\frac{B_t}{P_t}) = \Delta^f PV(s_t^f)$, moreover, $\Delta^f PV(s_t^f) = \Delta^f s_t^f + \Delta^i[\frac{B_{t-1}}{P_t} - s_t^f]$, which combine with the government's uses and sources of funds condition $(1 + i_t^S)R_t = \frac{B_t}{P_t} - \frac{B_{t-1}}{P_t} + s_t^f$ to give $\Delta^i(\frac{B_t}{P_t}) = \Delta^f s_t^f + \Delta^i[\frac{B_t}{P_t} - (1 + i_t^S)R_t]$. The last condition yields

$$R_t = \frac{\Delta^f s_t^f}{\Delta^i (1 + i_t^S)}$$

and substituting into the uses and sources of funds condition

$$\frac{B_t}{P_t} = \left[\frac{B_{t-1}}{P_t} - s_t^f \right] + \frac{(1 + i_t^S)\Delta^f s_t^f}{\Delta^i (1 + i_t^S)}$$

The optimal investment in the reserve funds R_t makes sure that the increase in returns after a fiscal shock is just enough to compensate for the shortfall in the primary surplus. The optimal perpetuity, on the other hand, is equal to this investment plus the historical level of debt. We will comment on this policy at the end of the next sub-section.

6.2 Income Shocks and Household Insurance

Households face idiosyncratic income shocks, such as unemployment or wage loss, that are not diversifiable within cohorts. To insure against these shocks, households pay premiums to insurance providers (or the government), which pool risk across cohorts

and invest in public debt. We model the insurance fund as holding a portfolio of bonds. If the fund invests in short-term debt, it faces rollover risk; if it invests in long-term debt, it faces liquidation risk. The optimal strategy balances these risks by matching the maturity structure of the fund's assets to the timing of expected payouts. This mechanism introduces a new redistributive channel: insurance premia are paid by all cohorts, but payouts benefit those experiencing shocks. The design of the debt portfolio affects the efficiency and equity of this redistribution.

Now introduce a simple change in the model. The problem we consider here is different from the above, in that households are subject to income shocks that they wish to insure. For each cohort there is an additional risk of income loss at every date after the first of $\delta W_{t,s}$ with probability v^I . This shock affects every member of the cohort in the same way and are distributed iid over time. Hence, it cannot be mitigated by within cohort insurance or contingent transfers. Insurance necessitates sharing the risk with other cohorts. The additional exposure to income losses can, however, be hedged by paying premia to an insurance company; or a government run scheme with the premia being a tax.

Let us suppose that the premia are paid across periods to smooth consumption. The income shock insurance is arranged by zero profit insurance companies, which take in and invest premia and make payments in the event of loss. Competition and actuarial fairness mean that the aggregate present value of these premia equals the present value of expected payouts. This element of social insurance means that there is sharing of income shocks across cohorts. This is modelled as an adjustment to the per-period wage income stream. The per-period budget constraint of a cohort is

$$C_{t,s} + \gamma E_t (\Lambda_{t,t+1} \frac{Z_{t+1} A_{t+1,s}}{\gamma}) + \gamma \frac{M_{t+1,s}}{P_t} =$$

$$\frac{Z_t A_{t,s}}{\gamma} + (1 + i_t^M) \frac{M_{t,s}}{P_t} + [W_{t,s} (1 - \delta_t) + X_{t,s} - V_{t,s}^{**} - T_{t,s}]$$
(53)

The income shocks are offset by payments of $X_{t,s}$. The expected value of the income shocks is $\sum_{\tau=0}^{\infty} \gamma^{\tau} v^I E_t(\Lambda_{t,t+\tau} \delta W_{t+\tau,s})$. The present value of premiums $V_{t,s}^{**}$, is $\overline{V}_{t,s}^{**} = \sum_{\tau=0}^{\infty} \gamma^{\tau} E_t(\Lambda_{t,t+\tau} V_{t+\tau,s}^{**})$, where $V_{t+\tau,s}^{**}$ is constant.

The optimal way of meeting the contingent needs of the insurance company to be able to cover the income losses is through a holding of (Arrow-Debreu) state-contingent claims. We assume that this is not possible and that insurance companies take in premia and pool risks and invest in bonds of a limited range of maturities. If an insurance company has sufficient reserves to meet current income losses that would allow the appropriate cover. Such an insurance company would then be in a position to take in premia and offer to cover losses on a fair basis. The reserves of the fund could be held in long-term bonds with some being liquidated in the event of a negative shock. If the initial endowment of the insurance fund is an issue, then a government run scheme, where the initial balance of the fund is obtained by issuing long-term bonds and servicing the debt with additional premium type taxation may be appropriate.

Suppose that the insurance premiums and any reserves of the insurance fund are

held in a portfolio of perpetuities, which insulates the insurance fund from any period by period variations in the short-term rate of interest. Then, if an income shock occurs, the insurance company must liquidate bonds to cover the loss. However, in the absence of liquidity risk, low prices for bonds at this date, there is no cost to this strategy. Suppose on the other hand, that the insurance company invests in one-period bonds. Then, in the event of a loss it uses the realised value of some one-period bonds to cover the loss. In the event that the loss does not occur it rolls-over the bonds by purchasing new ones. If there is no exposure to roll-over risk from rising short-term interest rates, there is no cost to this strategy. Hence it is a matter of indifference which strategy is used.

There is the possibility that at each date the short-term interest rate jumps. At each date there is a potential shock to interest rates, they may jump up by $\Delta^i i_t^S$, then holding short-term bonds may be expensive. This arises as the one-period cost of the strategy includes a refinancing cost if the bonds are not needed with probability $(1-v^I)$ to fund payouts, this cost is $\Delta^i i_t^S B_t^{S*}$. On the other hand, if liquidating long-term bonds with probability v^I may be expensive because of of the impact of a negative liquidity effect on liquidated bonds of $\Delta^I B_t^{L*}$. Given that the probability of the liquidity event is exogenous, the choice of strategy involves a simple comparison of $(1-v)\Delta^i i_t^S B_t^{S*}$ to $v\Delta^I B_t^{L*}$. Given that this is loss is possible at every date, this comparison arises at every date. So if the cost of roll-over risk is greater than liquidation cost risk, it means that it is optimal to hold enough short-term bonds in reserve to meet current needs and hold longer-term bonds, perpetuities, as reserve to meet later needs as they arise.

Here we note that Kosar et al. (2024) use detailed microdata to show that households frequently use fiscal transfers to repay debt, especially those with high debt burdens. Their findings suggest that fiscal policy acts as a form of insurance against income volatility, with long-run effects on consumption smoothing. This validates our model's mechanism where income shocks are mitigated through intertemporal redistribution via public debt instruments.

6.3 Policy Implications

Both fiscal and income shock insurance rely on the government's ability to issue debt instruments that span the relevant state space. In practice, this means: diversifying maturities to hedge against different types of risk; using perpetuities to smooth long-term liabilities; and maintaining reserves to buffer short-term shocks. In both cases the crucial issue is to smooth the impact of the shocks and avoid short-term exposure to interest rate risk. However, funding the government budget or the insurance schemes portfolio with long-term bonds, perpetuities, does impose a burden on yet unborn cohorts and will other-things-being equal increase consumption relative to what it otherwise would be. In the case of income shocks, the trade-off may involve considering the convex costs of rollover-risk against the liquidation risk associated with long-term bonds. These strategies enhance macroeconomic stability and intergenerational fairness. However, they also impose burdens on future cohorts, raising normative questions about sustainability and

equity.

7 Evaluating Efficiency and Welfare

This section evaluates the efficiency properties of the model, focusing on steady-state outcomes. We examine whether fiscal and monetary policies improve welfare in the presence of overlapping generations, heterogeneous agents, and incomplete markets. The analysis builds on the Phelps-Koopmans criterion and incorporates insights from Diamond (1965), Tirole (1985), and Barro (1974).

7.1 Dynamic Efficiency and Overaccumulation

In the baseline model with log utility, savings behavior is governed by the relationship between the real interest rate and the rate of time preference. If the real interest rate falls below the growth rate of the economy, the economy may be dynamically inefficient—leading to overaccumulation of capital and suboptimal consumption. Government debt and money holdings can improve efficiency by crowding out excess capital. Debt-financed transfers to current cohorts reduce savings, raise the real interest rate, and restore optimal capital levels. This mechanism mirrors the classical Diamond result, where public debt acts as a corrective instrument in an inefficient equilibrium.

We first examine some basic efficiency properties of the model. Blanchard (1986) undertakes an evaluation of the efficiency of his model in which he examines its dynamics and steady state properties. Here, we undertake similar exercises but only examine the steady state. As in Diamond (1965) and Blanchard we consider Phelps (1961)-Koopmans (1965) efficiency. It is easier to make the main point using the special case of log utility in which $\alpha = 1$. Note that savings is given by

$$S = (Y - T) - C \tag{54}$$

Substituting for consumption and income as Y = W + rQ. Letting $\beta = 1/1 + \rho$, and approximating $[1 - \beta\gamma] \approx \rho + (1 - \gamma)$, which is exact in the limit of continuous time:

$$S = W + rQ - (\rho + (1 - \gamma)) \left[\frac{W}{r + (1 - \gamma)} - \overline{T}_t + Q + \frac{B_t}{P_t} + \frac{\overline{M}}{P_t} \right]$$
 (55)

Collecting terms

$$S = W \frac{[r - \rho]}{(r + (1 - \gamma))} + Q[r - \rho - (1 - \gamma)] - (\rho + (1 - \gamma))[-\overline{T}_t + \frac{B_t}{P_t} + \overline{\frac{M}{P_t}}]$$
 (56)

Let the fiscal and monetary terms $\overline{T}_t = \frac{B_t}{P_t} = \overline{M}_t = 0$. On a balanced growth path on which $S_t = I_t$ with $K_t = K_{t-1}$, so $I_t = \delta K_{t-1}$. The solution must lie between two values of $K: r(K^*)$, which satisfies $r(K^*) \cong \rho$; and $r(K^{**}) \cong \rho + (1 - \gamma)$.

The modified golden rule solution obtains when $\gamma = 1$ and $T_t = Q = \frac{B_t}{P_t} = \frac{\overline{M}}{P_t} = 0$ and r satisfies $r(\hat{K}) = \rho$. In the absence of trade with unborn generations, or current

generations caring in the sense of Barro (1974) about future generations through a bequest motive, the equilibrium interest rate in the model in the paper may well be below $r(\hat{K})$.¹¹ Then alternative assets can improve efficiency by reducing capital holding. Some level of money holding will substitute for over-accumulation of capital as will holding government bonds of any maturity structure, so long as some of the implied tax liabilities fall on unborn cohorts. That is some degree of financial crowding out will increase welfare in well understood ways. Let us address these issues below.

7.2 Bubble-Like Features of Government Debt

In economies with finite lives and incomplete markets, government debt can exhibit bubble-like properties. Households value debt based on expected tax liabilities, but the government can roll-over debt indefinitely, effectively taxing resources "at infinity." This creates a wedge between household and government transversality conditions. Following Tirole (1986) and Gali (2014 and 2020), we interpret government debt as a store of value that transfers purchasing power across generations. In this setting, debt issuance can raise welfare by reallocating resources from unborn to current cohorts, especially when markets fail to internalize intergenerational trade.

The extent to which money holding can increase and displace capital in portfolios is limited by the demand for money and requires setting interest rates lower. A lower nominal interest rate target cannot be separated from the inflation target, so this necessarily involves reducing the inflation target. Turning to debt financing, this can only displace capital if the debt constitutes net wealth as in the original Diamond formulation. However, there is an additional avenue which concerns a bubble-like feature of government debt as examined by Tirole and Gali as well as others.¹²

From a household's perspective, the transversality conditions on their lifetime budget constraint (infinite horizon but finite life expectancy) is satisfied inclusive of the taxes they expect to pay. However, from the government's perspective, if the economy is dynamically inefficient there is value at infinity. Households are not able to access this value by issuing securities, but the government can. Hammond (1975) examined the problem as a poverty, or isolated generation game, that can be understood along the lines of Samuelson (1958) and Shell (1971).¹³ Transfers of value from infinity through

 $^{^{11}}$ Barro (2020) notes that the general Phelps-Koopmans efficiency condition that the riskless rate exceeds the growth rate, r > g, does not hold in data (see Abel et. al. (1989) and Blanchard (2019)). However, he argues that the condition holds when r is based on risky returns (on equity) but not when r is based on safe returns (approximated by treasury bills). He argues that in a stochastic growth model r is replaced by a risky expected return that incorporates a significant equity premium. To resolve the equity-premium puzzle of Mehra and Prescott (1985), he uses a simple model with disaster risk based on Rietz (1988) and Barro (2006).

¹²The concern of this paper is closest to that of Tirole. Gali is concerned with showing the existence of bubbles and then showing how the random fluctuation in the value of bubbles impacts output in a model with some price stickiness and hence a stochastic output gap.

¹³Shell (1971) give a simple illustration of Samuelson's (1958) problem using a chocolate bar economy analogy. The economy consists of a infinite sequence of two-period overlapping generations. Each generation is born with one bar of a perishable good. An autarkic solution is overcome by a sequence of IOU's, which facilitates trade between generations. If this works, the IOU each period is exchanged for the perishable good and so every generation to infinity has consumption when young and old except for the first, which gets the bonus of being able to consume all of its endowment when young. This additional

sequences of IOUs may be sustainable in a super-game setting but if not then a social security or inter-temporal tax-based redistribution scheme may be effective. In its most stark form government debt is essentially interest-bearing money (pieces of paper). The payments of interest in an inefficient economy can be made by essentially taxing resources trapped at infinity. In this case households place a finite capital value on their expected tax liabilities, but the government can finance repayment of debt by rolling over debt and hence tax payments to infinity.¹⁴ Then, it is this feature of debt as opposed to taxing unborn generations, that increases efficiency. Note that in inefficient equilibria with bubble values, the transversality condition on the government's inter-temporal budget constraint is not satisfied, so that the equation cannot be used to define a unique price level as an equilibrium outcome.

7.3 Agent Heterogeneity and Redistribution

The presence of agent heterogeneity, as illustrated in the model implies that fiscal and monetary policies have distributional. consequences even in frictionless markets. For example, debt maturity affects impatient and patient agents differently, creating scope for targeted debt instruments. Similarly, as we have shown, income shock insurance redistributes across cohorts, raising questions about optimal premium design and intergenerational fairness. While some policies improve aggregate welfare, they may exacerbate inequality or harm constrained agents. A full welfare analysis must therefore consider both efficiency and equity, rather than defining social welfare across cohorts and types using a welfare aggregator this can be undertaken, as in Weretka and Dec (2021) using a Kaldor-Hicks framework of equivalent and compensating variations to assess whether winners could hypothetically compensate losers.

In our model we have examined a number of redistributive effects. Debt-financed tax cut change the intertemporal tax burden by redistributing to impatient agents (consume more now) at the expense of future cohorts. Lengthening debt maturity defers tax liabilities which benefits current cohorts at the expense of future cohorts. Increasing the inflation target causes real wealth erosion, benefiting borrowers at the expense of savers. Finally and more subtly income shock insurance leads to premium based transfers that

unit of consumption has essentially come from infinity and is the bubble value of the IOU. Every generation in the sequence is better of but there is a problem that every generation has a temptation to deviate and not accept the previous generation's IOU and issue their own IOU.

This led Hammond (1975) to consider the problem as a super game with punishments for those who do not honour IOUs. In his case the transfers between generations were pension payments but the problem is the same. However, his solution involves individuals yet unborn inheriting an understanding that they must punish coexisting generations if they failed to pay a fair pension by not paying them a fair pension or honour IOUs and thereby see the need to act the same way themselves.

Shell and others have suggested that the efficient solution and the value of the bubble is enforced by the government accepting the IOU as the only medium in which to settle tax liabilities.

¹⁴The Ponzi scheme nature of government finance described (see Barro 2020) assumes that the government can always meet required payments through taxes. This requires that the government remains solvent, so that the value of payments on debt must be bounded by the value of the governments tax base. Uncertainty in the evolution of GDP implies that the rolling-over forever of the government's debt generates a positive probability that the debt would eventually exceed the government's collateral, thereby triggering sovereign default. In this case, Ponzi borrowing in risk-free form by the government can be ruled out

benefit high income cohorts at the expense of low income cohorts.

7.4 A Second-Best Welfare Theorem

In order to capture the impact of these effects we state a second-best Welfare Theorem (a la Besley and Coate (2003)) for our overlapping generations model with heterogeneous agents and incomplete markets. The theorem is adapted to our setting where lump-sum transfers are constrained by cohort structure and market incompleteness.: "In an economy with overlapping generations, heterogeneous time preferences, and incomplete markets, any Pareto-efficient allocation can be decentralized via a combination of: a maturity-structured public debt policy; lump-sum taxes and transfers across cohorts, insurance premia for income shocks provided that the government can issue debt instruments that span the relevant state space and redistribute intertemporally." This theorem highlights the role of fiscal architecture in achieving welfare-enhancing outcomes, even when first-best instruments are unavailable.

To conclude, redistributive policies generate real welfare effects even in frictionless markets. The presence of agent heterogeneity amplifies these effects, especially when borrowing constraints bind or income shocks are asymmetric. Optimal policy design must therefore balance efficiency with equity, using debt maturity and insurance mechanisms to smooth intertemporal burdens."

8 Conclusion

This paper develops a dynamic framework for analyzing fiscal and monetary policy in an economy with overlapping generations, heterogeneous agents, and incomplete markets. By embedding redistributive motives and debt maturity structures into the model, we detail normative insights into the intertemporal trade-offs faced by policymakers.

In contemporary macroeconomic discourse, the real effects of fiscal and monetary policy are often attributed to nominal rigidities, aggregate demand fluctuations, or expectations management. Yet such approaches frequently overlook a more fundamental mechanism: redistribution. This paper reorients the analysis by demonstrating that even in a frictionless, forward-looking economy, fiscal and monetary interventions can have significant real consequences, not because they mislead agents, but because they reallocate resources across time and individuals. The central insight is that fiscal policy is inherently redistributive, and these redistributions have real effects even in the absence of nominal frictions. By comparing steady states across different fiscal regimes, the paper reveals how policy design shapes long-run economic outcomes. In doing so, it offers an alternative to conventional macroeconomic models and provides an alternative foundation for analyzing the real impacts of public finance.

The paper has developed a dynamic Metzleric model that incorporates Blanchard type intergenerational cohorts and an intertemporal government budget constraint. The model incorporates heterogeneity, with two types of individual born at each date, patient and impatient. Insurance markets are introduced to allow risks to be traded and to

provide a simplification of the model and to allow us to focus on some simple channels for the real effects of policy. The model is set up to provide a simple setting in which to investigate substituting tax for debt finance, changes in the maturity structure of government debt and inflationary finance. Real effects occur because of redistribution owing to finite horizons, incompleteness of markets and differential discount rates. The final section of the paper examines some simple efficiency properties of the market equilibrium and hence the basis for government intervention.

The paper offers a new perspective on how fiscal and monetary policy shape real economic outcomes, not through nominal frictions or aggregate demand channels, but through redistribution, asset structure, and intertemporal budget dynamics. Using an overlapping generations framework enriched with annuity contracts, unplanned bequests, and partial insurance against income shocks, it demonstrates that the design of public debt, especially its maturity structure, has significant implications for household behavior, wealth distribution, and macroeconomic stability. Crucially, the paper shows that fiscal policy is not neutral: debt-financed tax cuts, changes in debt composition, and default risk all redistribute resources across cohorts and asset holders. These redistributive effects influence consumption, savings, and investment decisions, even in the absence of nominal rigidities. The government's budget constraint is treated not as a pricing equation, but as an equilibrium "uses and sources of funds" condition within a full general equilibrium model—thereby avoiding the pitfalls of the "fiscal theory of the price level as critiqued by Buiter. The framework provides an alternative lens for analyzing long-run policy impacts through comparative steady states, offering insights into how fiscal architecture and monetary accommodation jointly shape economic outcomes. By focusing on real redistribution rather than nominal anchors, the paper attempts to bridge classical fiscal theory with modern concerns about inequality, debt sustainability, and policy design.

Dynamic inefficiency, manifested through over-accumulation of capital, can be corrected via public debt, restoring optimal consumption and investment levels. Government debt may exhibit bubble-like features, enabling intergenerational transfers without violating household budget constraints. A second-best welfare theorem demonstrates that efficient allocations can be decentralized through a structured combination of debt instruments, taxes, and insurance mechanisms. These findings challenge conventional macroeconomic models that treat redistribution as incidental. Instead, we argue that redistributive design is foundational to effective policy.

References

[1] Abel, Andrew B., N. Gregory Mankiw, Lawrence H. Summers, and Richard J. Zeckhauser, 1989, "Assessing Dynamic Efficiency: Theory and Evidence," Review of Economic Studies 56 (January), 1-19.

- [2] Angeletos, Marios, 2002, "Fiscal Policy with Non-Contingent Debt and the Optimal Maturity Structure," Quarterly Journal of Economics 117, 1105–1131.
- [3] Barro, Robert. 1974. "Are Government Bonds Net Wealth?" Journal of Political Economy, 81(6):1095–1117.
- [4] Barro, Robert J., 1979, "On the Determination of the Public Debt," Journal of Political Economy 87, 940–971.
- [5] Barro, Robert J., 1989, "The Neoclassical Approach to Fiscal Policy," in Robert J. Barro, ed., Modern Business Cycle Theory (Cambridge, MA: Harvard University Press, 1989), pp.1-15.
- [6] Barro, Robert J. 2006. "Rare Disasters and Asset Markets in the Twentieth Century." Quarterly Journal of Economics, 121 (August), 823-866.
- [7] Barro, Robert J. 2020. "r Minus g." CESifo Working Papers No. 8661.
- [8] Besley, Timothy, & Coate, Stephen. (2003). On the Public Choice Critique of Welfare Economics. Public Choice, 114(3–4), 253–273.
- [9] Blanchard, Olivier, 1985, "Debt, Deficits, and Finite Horizons. Journal of Political Economy, 93(April):223-247.
- [10] Blanchard, Olivier, 2019. "Public Debt and Low Interest Rates," American Economic Review 109 (April), 1197-1229.
- [11] Bohn, Henning, 1990, "Tax Smoothing with Financial Instruments," American Economic Review, LXXX, 1217-1230.
- [12] Buiter, Willem H, 1988, "Death, Birth, Productivity Growth and Debt Neutrality," The Economic Journal, 98, 279-293.
- [13] Buiter, Willem H, 2002, "The fiscal Theory of the Price Level: A Critique," The Economic Journal. 112, 469-480.
- [14] Calvo, Guillermo A, 1983, "Staggered Prices in a Utility-Maximizing Framework," Journal of Monetary Economics 12, Issue 3, 383-398.
- [15] Cadsby, Charles Bram & Frank, Murray (1991). Experimental Tests of Ricardian Equivalence. Economic Inquiry, 29(4), 645–664.
- [16] Chamley, Christophe and Herakles Polemarchakis, 1984. "Assets, General Equilibrium and the Neutrality of Money," Review of Economic Studies, 51, 129-138.
- [17] Cochrane, John. H. 2023. "The fiscal theory of the price level." Princeton University Press.
- [18] Diamond, Peter1965, "National Debt in a Neoclassical Growth Model," American Economic Review, 55(5-1):1126-1150.

- [19] Edwards, Jeffrey A. (2006). Politics, Inflation, and the Mundell-Tobin Effect. Journal of Economic Insight, 32(2), 9–30.
- [20] Farmer, Roger E. A., 2016, "Pricing Assets in an Economy with Two Types of People," NBER Working Paper 22228.
- [21] Fischer, Stanley.1979. "Anticipations and the Nonneutrality of Money," [Journa of Political Economy,vol. 87, no 2, 225-252.
- [22] Gale, Douglas. 1990. "The Efficient Design of Public Debt," In R. Dornbusch and M. Draghi (Eds.), Public Debt Management: Theory and History. Cambridge: Cambridge University
- [23] Galí, Jordi, 2014, "Monetary Policy and Rational Asset Price Bubbles," American Economic Review, vol. 104(3), 721-752
- [24] Galí, Jordi, 2020, "Monetary Policy and Bubbles in a New Keynesian Model with Overlapping Generations," NBER Working Paper 26796.
- [25] Greenwood, Robin, Samuel G Hanson, and Jeremy C Stein, 2015, "A Comparative-Advantage Approach to Government Debt Maturity" Journal of Finance vol LXX, NO. 4 1684-1722.
- [26] Guibaud, Stephane, Yves Nosbusch, and Dimitri Vayanos, 2013, "Bond Market Clienteles, the Yield Curve, and the Optimal Maturity Structure of Government Debt," Review of Financial Studies 26, 1914–1961.
- [27] Hammond, Peter. 1975. "Charity: Altruism or Cooperative Egoism?," (pp. 115-132) in "Altruism, Morality, and Economic Theory," Edited by Edmund S. Phelps. Published by: Russell Sage Foundation.
- [28] Isiaka, Abdulaleem; Mihailov, Alexander; Razzu, Giovanni (2024). Fiscal Policy and Inequality in Middle- and High-Income Countries: Redistributive Effects of Tax and Spending Shocks. Macroeconomic Dynamics, 29, e12.
- [29] Koopmans, Tjalling C. 1965. "On the Concept of Optimal Economic Growth," in The Pontifical Academy of Sciences, The Econometric Approach to Development Planning, Amsterdam, North Holland.
- [30] Kosar, Gizem; Melcangi, Davide; Pilossoph, Laura; Wiczer, David (2024). Stimulus through Insurance: The Marginal Propensity to Repay Debt. Federal Reserve Bank of Atlanta Working Paper No. 2024-14.
- [31] Levhari, David and Leonard J. Mirman. 1977, "Savings and Consumption with an Uncertain Horizon," Journal of Political Economy, vol. 85, no. 2.
- [32] Leeper, Eric. M, 1991,. "Equilibria under 'active' and 'passive' monetary and fiscal policies." Journal of Monetary Economics, 27(1), 129–147.

- [33] March, Christoph & von Weizsäcker, Robert K. (2020). Coordinating Intergenerational Redistribution and the Repayment of Public Debt: An Experimental Test of Tabellini (1991). Social Choice and Welfare, 55, 301–323.
- [34] Marini, Giancarlo, and Frederick van der Ploeg. Marini, Giancarlo, and Frederick van der Ploeg. (1988), "Monetary and Fiscal Policy in an Optimising Model with Capital Accumulation and Finite Lives." Economic Journal 98, 772-86.
- [35] Mehra, Rajnish and Edward C. Prescott, 1985, "The Equity Premium: A Puzzle," Journal of Monetary Economics, 15, 145-161.
- [36] Metzler, Lloyd. A. 1951. "Wealth, Saving, and the Rate of Interest," Journal of Political Economy, 59, 93-116
- [37] Mundell, Robert A. 1960. "The Public Debt, Corporate Income Taxes, and the Rate of Interest," Journal of Political Economy, Vol. 68, No. 6, 622-626
- [38] Mundell, Robert A., 1965. "Growth, Stability, and Inflationary Finance." Journal of Political Economy 73, 97-109
- [39] Norman, Ben and Wilems, David. (2025). "A game-theoretic foundation for the fiscal theory of the price level." Bank of England Staff Working Paper No. 1137.
- [40] Nosbusch, Yves, 2008, Interest Costs and the Optimal Maturity Structure of Government Debt, Economic Journal 118, 477–498.
- [41] Phelps, Edmund S., 1961. "The Golden Rule of Accumulation: A Fable for Growthmen," American Economic Review 51, 638-643.
- [42] Rietz, Thomas A., 1988, "The Equity Risk Premium: A Solution." Journal of Monetary Economics, 22 (July), 117-131.
- [43] Ross, S. A. 1976. Options and Efficiency. Quarterly Journal of Economics. 90, 75-89
- [44] Samuelson, Paul A, 1958, "An Exact Consumption-Loan Model of Interest With or Without the Social Contrivance of Money." Journal of Political Economy, 66(6): 467–82.
- [45] Samuelson, Paul A., 1969, "Lifetime Portfolio Selection by Dynamic Stochastic Programming." Review of Economics & Statistics, 51, 239-246.
- [46] Sargent, Thomas. J., and Neil Wallace, N, 1981, "Some unpleasant monetarist arithmetic." Quarterly Review, Federal Reserve Bank of Minneapolis, 5(Fall), 1–17.
- [47] Shell, Karl. 1971. "Notes on the Economics of Infinity," Journal of Political Economy, 79(5): 1002–1011.
- [48] Sidrauski, Miguel, 1967, "Rational Choices and Patterns of Growth in a Monetary Economy." American Economic Review, 57, 534-544.

- [49] Sims, Christopher. A, 1994, "A simple model for study of the determination of the price level and the interaction of monetary and fiscal policy." Economic Theory, 4(3), 381–399.
- [50] Stiglitz, Joseph E., 1969, "A Re-Examination of the Modigliani-Miller Theorem," The American Economic Review, 59, No. 5, 784-793.
- [51] Tabellini, Guido (1991). The Politics of Intergenerational Redistribution. Journal of Political Economy, 99(2), 335–357.
- [52] Tirole, Jean 1985, "Asset Bubbles and Overlapping Generations," Econometrica 53, 1499-1528.
- [53] Tobin, James, 1965, "Money and Economic Growth," Econometrica, XXXIII, No. 4, 671-84.
- [54] Wallace, Neil, 1981, "A Modigliani-Miller Theorem for Open-Market Operations", American Economic Review, 71(3), 267-274.
- [55] Weretka, Marek & Dec, Marcin. (2021). Welfare Measurements with Heterogeneous Agents. GRAPE Working Paper No. 50, Group for Research in Applied Economics.
- [56] Woodford, Michael 1995, "Price Level Determinacy Without Control of a Monetary Aggregate," Carnegie-Rochester Conference Series on Public Policy. 43: 1–46
- [57] Woodford, Michael, 2001, "Fiscal Requirements for Price Stability," Journal of Money Credit and Banking 33 (3): 669-728.
- [58] Woodford, Michael, 2003, "Interest and Prices: Foundations of a Theory of Monetary Policy," Princeton University Press, Princeton, N.J.

34