## Economic Growth in a Cooperative Economy

Thomas Brzustowski and Francesco Caselli

## Backlash against Capitalism

#### Politics

- Leftward shift (of leftist parties)
- Re-legitimization of "socialism"
- Academia and Public Intellectuals
  - Tsunami of "Crisis of Capitalism" books
  - Proposals to reform corporate governance
    - Employee role in management ("Democratizing Work")
    - Dropping "shareholder value"
    - Rethinking the corporation's purpose

Dynamic model of a cooperative-based economy

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    - GE challenge: Allocation of workers to coops

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  - Qualitative features of growth path and steady state

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    - Dynamic challenge: Capital accumulation
    - GE challenge: Allocation of workers to coops
  - Qualitative features of growth path and steady state
  - Quantitative comparison with corporation-based economy

## Economic Literature on Cooperatives

Cooperative size and static efficiency in PE

- Ward (1958, 1967), Domar (1966), Hansmann (1996)
- Existence and Pareto Optimality in GE
  - Vanek (1970), Laffont and Moreaux (1983), Dreze (1989)
- Worker heterogeneity and incentives
  - Kremer (1997), Levin and Tadelis (2005)
- Pooled Investment
  - Rey and Tirole (2007)
- Consumer cooperatives
  - Hart and Moore (1996, 1998)

## Institutional Differences

	Capitalism	Cooperativism
Firm objective	max profits	max utility
Capital ownership	individuals	cooperatives
Capital market	yes	no
Labour market	yes	yes
Product market	yes	yes
Free entry	yes	yes

#### Problem: present bias

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  - Two-period OLG framework

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- Modelling implication
  - Two-period OLG framework
    - Infinite horizon alternatives either very complicated (tracking workers through cooperatives) or uninteresting (lifetime attachment)

## **Physical Environment**

- Demographics: constant cohorts of measure L
- ▶ Life cycle: work as *Y*, consume as *Y* and *O*
- ▶ Preferences:  $U(c^Y, c^O)$
- Technology: F(k, l)

## Capitalist Economy

 $\max_{k,l} \{F(k,l) - r_t k - w_t l\}$ 



Firms

$$\max_{c_t^Y, c_{t+1}^O} U(c_t^Y, c_{t+1}^O)$$

$$c_t^Y = w_t - \kappa_{t+1}$$
$$c_{t+1}^O = r_{t+1}\kappa_{t+1}$$

Market clearing and free entry

## Cooperative concept

• Coop with  $l_t$  young workers,  $l_{t-1}$  former workers, capital  $k_t$ 

$$c_{t}^{Y} = \frac{F(k_{t}, l_{t}) - T_{t} - k_{t+1}}{l_{t}}$$
$$c_{t+1}^{O} = \frac{T_{t+1}}{l_{t}}$$

Simplifying assumption

$$T_t = \tau F(k_t, l_t)$$

Literal interpretation: legal requirement, articles of association
 Broader interpretation: inter-generational social security game
 Removes l<sub>t-1</sub> as a state variable

## Investment decision

• Coop with  $I_t$  young workers, capital  $k_t$ 

$$\max_{k_{t+1}} U(c_t^Y,c_{t+1}^O)$$

$$c_{t}^{Y} = \frac{(1-\tau)F(l_{t}, k_{t}) - k_{t+1}}{l_{t}}$$
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▶ Next: Determination of  $l_t$ ,  $l_{t+1}$  (allocation mechanism)

- It incumbent cooperatives, with
- ► k<sub>it</sub> capital
- ► *l<sub>it-1</sub>* former workers

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- Production, Investment decision, Payments to young and old workers

## Equilibrium selection

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Implication

$$\left(\mathcal{L}(k_{it}), \mathcal{K}(k_{it})\right) \in \arg\max_{l,k} U\left(\frac{(1- au)F(l,k_{it})-k}{l}, \frac{ au F\left(\mathcal{L}(k),k\right)}{l}\right)$$

k and l trade offs

## Example

Technology (Incumbents)

$$F(k, l) = Ak^{\alpha}(l - \underline{l})^{\beta} \quad \alpha + \beta < 1$$

# Fixed cost Decreasing returns to variable inputs (Entrants use some technology G(I))

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Fixed cost
 Decreasing returns to variable inputs
 (Entrants use some technology G(I))
 Preferences

$$U(c^{Y}, c^{O}) = \log c^{Y} + \delta \log c^{O}$$

# Capitalist equilibrium

$$\begin{split} l_t &= \frac{1-\alpha}{1-\alpha-\beta} \underline{l} \equiv l_{cap} \\ \kappa_{t+1} &= \frac{\delta}{1+\delta} A (1-\alpha)^{\alpha} \beta^{\beta} \Big( \frac{1-\alpha-\beta}{\underline{l}} \Big)^{1-\alpha-\beta} \kappa_t^{\alpha} \end{split}$$

# Cooperative Equilibrium

$$I_{t} = \frac{1+\delta}{1+\delta-\beta(1+\delta\alpha)} \underline{I} \equiv I_{coop}$$
$$k_{t+1} = \frac{\delta\alpha}{1+\delta\alpha} (1-\tau) A \left(\frac{\beta(1+\delta\alpha)}{1+\delta-\beta(1+\delta\alpha)} \underline{I}\right)^{\beta} k_{t}^{\alpha}$$

## Steady state convergence

- Subject to restrictions on G(I) ... Details
- ▶ ... For any initial  $\{k_{i0}\}$  converge to steady state with

$$I_i^* = I_{coop}, \text{ all } i$$

## Firm Size and Static Efficiency

Static social planner problem

$$\max_{l} \quad \frac{L}{l} F\left(\frac{K}{L/l}, l\right)$$

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equiv.  $Z_{eff} = Z_{cap} \ge Z_{coop}$ 

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► Sources of inefficiency  
► 
$$\delta = 0$$
  
 $I_{eff} = \frac{1 - \alpha}{1 - \alpha - \beta} \underline{l} \ge \frac{1}{1 - \beta} \underline{l} = I_{coop}$   
►  $\alpha = 0$   
 $I_{eff} = \frac{1}{1 - \beta} \underline{l} \ge \frac{1 + \delta}{1 + \delta - \beta} \underline{l} = I_{coop}$ 

Capital Accumulation and Dynamic Efficiency

Golden Rule saving

$$\max_{s} \{Y_{eff}(L,K) - sY_{eff}(L,K)\} \quad s.t. \quad K = sY_{eff}$$

•  $s_{gold} = \alpha$ • Equilibrium saving rates •  $s_{cap} = \frac{\delta}{1+\delta}(1-\alpha)$ •  $s_{coop} = \frac{\delta\alpha}{1+\delta\alpha}(1-\tau)$  Capital Accumulation and Dynamic Efficiency

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Cooperative economy dynamically efficient

$$s_{coop} \leq s_{gold}$$

### Steady State Output

If symmetric steady state

$$rac{Y^*}{L}=(s^*)^{rac{lpha}{1-lpha}}(Z^*)^{rac{1}{1-lpha}}$$

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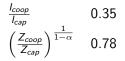
# Quantification (log utility case)

Parameter	Target	Data	Value
α	rK/Y	0.33	0.33
$\beta$	<u>I</u> /I	0.18	0.55
$\delta$	K/Y	3/25	0.22

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$$\begin{pmatrix} \frac{l_{coop}}{l_{cap}} & 0.35\\ \left(\frac{Z_{coop}}{Z_{cap}}\right)^{\frac{1}{1-\alpha}} & 0.78 \end{cases}$$

S <sub>cap</sub>	0.12
S <sub>coop</sub>	0.06
$\left(rac{s_{coop}}{s_{cap}} ight)^{rac{lpha}{1-lpha}}$	0.71

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 $\frac{Y_{coop}}{Y_{cap}}$ 

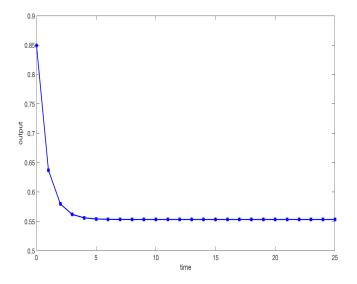
0.55

# Thought Experiment

 $\blacktriangleright$  at  $t_0$  capitalist steady state

▶ at  $t_1$  capital redistributed to  $N = L/I_{coop}$  cooperatives

# Dynamics of Output



#### Welfare Loss

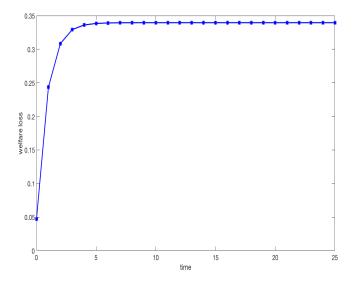
Equivalent variation

$$U(c_{t,coop}^{Y} + X_t, c_{t+1,coop}^{O} + X_t) = U(c_{*,cap}^{Y}, c_{*,cap}^{O})$$

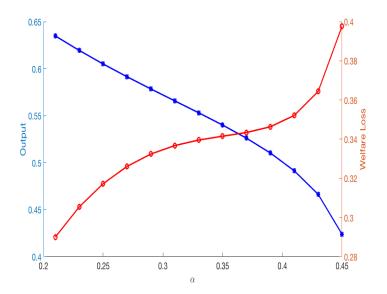
► Welfare loss

$$2X_t/(c_{*,cap}^Y+c_{*,cap}^O)$$

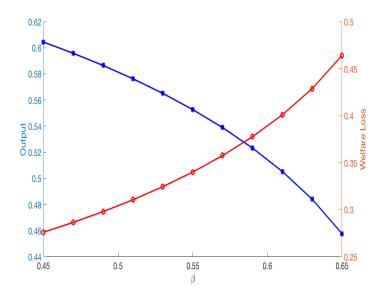
### Dynamics of Utility



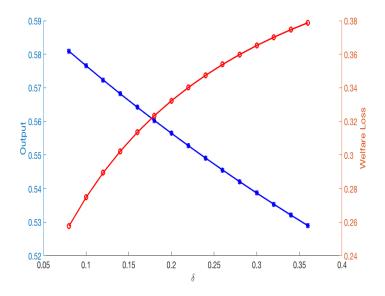
### Robustness: $\alpha$



#### Robustness: $\beta$



#### Robustness: $\delta$



#### Example 2

Same technology but

$$U(c^{Y}, c^{O}) = \frac{(c^{Y})^{1-\sigma}}{1-\sigma} + \delta \frac{(c^{O})^{1-\sigma}}{1-\sigma}$$

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$$U(c^{Y}, c^{O}) = \frac{(c^{Y})^{1-\sigma}}{1-\sigma} + \delta \frac{(c^{O})^{1-\sigma}}{1-\sigma}$$
$$\sigma = 2$$

### Calibration

			log	IES = 2
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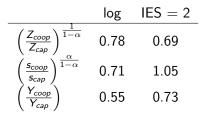
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au	Max U		0.12	0.15

### Quantitative Implications



### Conclusions

Dynamic extension of models of cooperative production

- To do (this paper)
  - Institutional variations
    - Inter-cooperative capital market
    - Self-management with private ownership
  - Coexistence
  - Money, Social Security
  - Endogenize au
- To do (next paper(s))
  - Richer model with microeconomic heterogeneity
  - Quantify inequality-efficiency trade off

# Restrictions on G(I)

- ► Assumption 1:  $U_e \leq U(k_{coop}^*)$
- ► Assumption 2:  $\mathcal{L}_e \geq I_{coop}$
- Assumption 3:  $U_e \leq U(\mathcal{K}_e)$

Example

$$F(0, I) = B(I - \underline{I}_e)^{\gamma},$$

► For 1 and 3: *B* small  
► For 2:  

$$\gamma \in (0, (1 + \alpha)/(1 + \alpha\delta)),$$

$$\underline{l}_{e} \geq [1 + \delta - \gamma(1 + \alpha\delta)] / [1 + \delta - \beta(1 + \alpha\delta)] \underline{l}$$

