From MOS to eMOS Generalising Model Output Statistics for Full Ensemble Forecasts

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- EPS raises another issue: The process generating the ensemble variation is not the same as the process underlying forecast uncertainty.
 - Our predictions may also benefit from a more sophisticated interpretation of the ensemble.
- We introduce the idea of "ensemble MOS" a method of interpreting ensembles that conditions the forecast on the *joint* information present in the whole ensemble, rather than interpreting each ensemble member individually as a "scenario".

Given: only the model-wet/dry event (whether model-precip is more or less than 0mm) Forecast: probability of precip > 0mm in an actual rain gauge. (We use the one at WMO10015.)

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- We will investigate three different methods of producing the forecast from the ensemble of model-wet/dry events:
 - 1. Direct interpretation; model-precip and weather-precip are treated as identical. The forecast probability for real-precip is the proportion of model-wet events in the ensemble.

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 - 2. Scenario MOS; a separate forecast probability is made for each ensemble member. These are then combined.

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 - 2. Scenario MOS
 - 3. Ensemble MOS (eMOS); the forecast is a function of the joint distribution of the *whole* ensemble.

Simplified Example: Direct Interpretation



- Ignorance is log f(x), where f(x) is the forecast probability of the outcome x. Smaller ignorance relative to climatology or another forecast is better.
- The confidence intervals are ±1 bootstrap std. dev.

Ensemble members are interpreted as equally plausible scenarios:

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Ensemble members are interpreted as equally plausible scenarios:

- 1. For each ensemble member (model-wet/dry) a probability forecast scenario is created. For example:
 - model-wet could correspond to a 50% chance of precip (and, of course, 50% chance of no precip), while
 - model-dry corresponds to a 5% chance of precip (and 95% chance of no precip).

These actual percentages chosen are the parameters of our scenario MOS.

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- 2. The forecast is the average of all the scenarios.
- 3. The parameters are tuned to minimise the forecast's ignorance on a historical data-set.



- In contrast to the direct interpretation, performance is now better than climatology.
- Skill generally improves with shorter lead times.

Idea: ensemble MOS

Any forecast method is a function from the ensemble to the forecast probability:

Scenario MOS:

Ensemble $\xrightarrow{\text{MOS}}$ Scenarios $\xrightarrow{\text{Combine}}$ Forecast

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• Going through the intermediate stage of a scenario forecast corresponding to each ensemble member can be a strong constraint on the types of forecast functions possible.

• The information present in the ensemble is just the number, #wet, of "wet" members.

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Direct interpretation is, essentially, the identity.

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Scenario MOS chooses the best linear predictor.

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An eMOS method can choose a non-linear predictor.

• The method of analogues can be used to fit the eMOS function:



Predicted probability of precip is the proportion of historical cases with precip at nearby #wet values.



 Interpreting the ensemble as a whole leads to significant improvements in skill over scenarios in the 1–7 day range.

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- Interpreting the ensemble as a whole leads to significant improvements in skill over scenarios in the 1–7 day range.
- This is clearly seen by comparing the two models directly rather than to climatology.

 There is more information in each ensemble member than just whether it was "wet" or "dry".
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- Can summarise the distribution by (say) its 10%, 50%, and 90% quantiles (p_{10} , p_{50} , and p_{90}).

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- Can summarise the distribution by (say) its 10%, 50%, and 90% quantiles (p₁₀, p₅₀, and p₉₀).
 And fit a function from this information into the probability of real precipitation:

 $(p_{10}, p_{50}, p_{90}) \mapsto$ probability of real precip



 Using the extra information results in large improvement at shorter lead-times.



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- As the threshold increases, skill over climatology decreases.
- This might be due to the small number of examples of > 10 mm precip in the training period — only about 6 occur.

• There is information in ensembles that can be extracted by considering their *joint* information rather than as just scenarios.

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- There is information in ensembles that can be extracted by considering their *joint* information rather than as just scenarios.
- eMOS looks for general relationships between forecast information and verification.
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- Forecast-verification archives of sufficient size are essential.

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- Forecast-verification archives of sufficient size are essential.
- eMOS makes no strong assumptions about the "meaning" of the information it uses — it can be easily extended to combine information from different sources.