

# On the Possibility of a Preference-based Power Index: The Strategic Power Index Revisited

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This paper will be presented at the Leverhulme Trust sponsored *Voting Power in Practice* Symposium held at the London School of Economics, 20-22 March 2011.

**Abstract.** In this paper we discuss the *strategic power index* (SPI) as we have developed in earlier work. In contrast to traditional power indices, which deduce power from voting rules for a set of players, the SPI employs the analytical tools of non-cooperative game theory. Actor preferences, the policy space, decision-making rules, as well as the strategic considerations of the players in playing games, are integrated into the analysis. While traditional power indices calculate the probability of a voter being decisive in a committee, the SPI measures average (expected) success. In view of various objections made against the SPI, we show that this index expresses power in a meaningful way. We argue against the idea that SPI as preference-based index is impossible since it does not capture ‘a fixed core of meaning of power’. We challenge the view that the index confounds power and success, and even can become negative. Finally, we discuss the proposition that the SPI is nothing but a modified Banzhaf index, and show that this proposition is based on a too simple representation of a strategic game.

**Key words:** a priori voting power, decision procedure, power indices, spatial voting, strategic power

## 1. Introduction

The purpose of this paper is to take issue with the critique raised against the *strategic power index*. The *strategic power index* (hereafter SPI) is a new method for evaluating the distribution of power in policy games. Conventional power indices, such as the Banzhaf, Shapley-Shubik and others, take the set of players and the bare decision-making rules as their domain and measure voting power by the extent to which a player in any collective body that makes yes-or-no decisions by vote may turn a losing coalition into a ‘winning’ coalition for all mathematically possible permutations of players (Shapley-Shubik index), or the relative number of times a

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player is decisive in a vote (Banzhaf index).<sup>2</sup> As mentioned in Felsenthal and Machover (1998), conventional voting power analyses are either based on cooperative games<sup>3</sup> or are entirely probabilistic measures.<sup>4</sup> What is measured by these indices is *a priori* power. By doing this, conventional power indices do not take account of positive or negative correlations of players preferences.<sup>5</sup> Critiques also point to the limited capability of traditional power indices to model players' strategic interaction and a complicated institutional structure typical for real world decision-making (see Garrett and Tsebelis 1997, 1999 a, b; Steunenberget al. 1996, 1997, 1999; Schmidtchen and Steunenberget al. 2002).

In contrast to those traditional power measures, the SPI rests on a notion of power as the ability "to get what you want". It is measured by the expected or average distance between players' ideal points and the equilibrium outcome in policy games in which players have different abilities to affect the final outcome of the decision-making procedure (Steunenberget al. 1999; Steunenberget al. 1996, 1997; Schmidtchen and Steunenberget al. 2002). The smaller the expected distance between a player's ideal points in the policy space and the equilibrium outcomes, the more power is attributed to a player compared to a 'neutral' player that does not have any decision-making rights in the game. This comparison with a 'neutral' or dummy player helps to differentiate between a player's success in a game and luck. Since a dummy player will be sometimes lucky by finding himself close to the equilibrium outcome, he also has a distance value in these games. Since a dummy player is impotent, his performance determines a baseline

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<sup>2</sup> These 'classical' indices have been supplemented with more recent power measures, such as the Johnston index, the Deegan-Packel index and the Holler index. The main differences between these indices are the ways in which coalition members share the benefits of their cooperation, and the kind of coalition players chose to form (see Colomer 1999). For a comparative investigation of traditional power indices see Felsenthal and Machover (1998), Holler and Owen (2001) and Laruelle and Valenciano (2008).

<sup>3</sup> For example, the Shapley-Shubik index measuring what Felsenthal and Machover call P-power, which posits an office-seeking motivation of voting behavior (see Felsenthal and Machover 1998: 171).

<sup>4</sup> See Penrose (1946), Banzhaf (1965), Coleman (1971, 1986), which take a policy-seeking viewpoint focusing on the degree to which a member's vote is able to influence the outcome of a vote. These indices reflect I-power in the sense of Felsenthal and Machover (1998: 36).

<sup>5</sup> That is not to say that traditional power indices are unable to take account of voters' preferences or spatial voting (see Straffin 1994). In probabilistic characterizations of voting power indices each voter  $i$ 's probability  $p_i$  of voting "yes" on a proposal is a random variable. Taking the  $p_i$  as an indicator of the acceptability of a proposal to voter  $i$  (see Straffin 1994: 1137), homogeneous as well as heterogeneous preferences can be modelled. If each  $p_i$  is chosen independently from the uniform distribution on  $[0,1]$  we have the Banzhaf index. The independence assumption means that the acceptability of a proposal to voter  $i$  is independent of its acceptability to any other voter  $j$  (see Straffin 1994: 1137). Note, that  $p_i = 1/2$ , which means that voter  $j$  voting "yes" is similar to flipping a coin. Note further, that the probability characterization of the Banzhaf index is restricted to its non-normalized version. If random variable  $p$  is chosen from the uniform distribution on  $[0,1]$ , and  $p_i = p$  for all  $i$  (homogeneity assumption), we have the Shapley-Shubik index. Here the acceptability of a proposal is the same to all voters.

above which we can speak of power. Secondly, we focus on distributions of state of the world, that is, various combinations of preferences and initial policies (status quo points), so that the index expresses expectations to level out the effect of luck in a different way that is, being close to the equilibrium outcome in a specific game. The intuition is that the power of a player resides only in the game form or the rules of a game and not in the way a specific game is played.

Whereas traditional power indices are based on the notion that players need to form some kind of majority or winning coalition, this new method of power measurement employs the analytical tools of non-cooperative game theory. Actor preferences, the policy space, as well as the rules of the decision-making process, are fully integrated into the analysis. Since it allows players to act strategically, this index is labeled the *Strategic Power Index*.<sup>6</sup>

The SPI gave rise to several comments in the literature. Garrett and Tsebelis (1999 b) argue that the SPI - although an improvement compared to conventional indices - nevertheless suffers from a drawback generated by the statistics used in it. Felsenthal and Machover (2001) proved a theorem stating that the SPI is a modified Banzhaf index. Napel and Widgren (2004: 519) give credit to it being the first unified approach to the measurement of decision-making power in that it combines an ex post analysis of well defined games with the ex ante prospect of being successful in the game form underlying these games. However, this first attempt to provide such a framework is considered to be “problematic”. Napel and Widgren (2004: 524) point to a potential for confounding power and success “that may, but need not, result from it”. In an earlier paper, they speak of a confusion of cause and effect (Napel and Widgren 2002: 2). They claim that “(o)nly for particular distribution assumptions ... luck (is) ‘leveled out’ by taking averages” (Napel and Widgren 2004: 524). The SPI is judged to be “a good measure of expected success but in general, it fails to capture power” and it may even become negative (Napel and Widgren 2004: 524). A fundamental critique has come from Braham and Holler (2005) who deny the possibility of a preference-based power index on the ground that it is incompatible with “a fixed core of meaning of power”, i.e., the basic notion of power as a generic ability.

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<sup>6</sup> This index was presented, in non-normalized form, for the first time in 1996 (see Steunenbergh, Koboldt and Schmidtchen 1996). It has been used to measure the distribution of power in the European Union. There is another attempt to develop a strategic power index labelled *strict power index* (Widgren and Napel 2001). As with our index, spatial preferences and strategic agenda setting are its main building blocks. However, in the framework of the strict power index power is defined as the ability of a player “to change the current state of affair” (Widgren and Napel 2001: 4). Following the reasoning of traditional power indices power relates to the ability of being decisive or pivotal.

This paper contains our responses and is organized as follows. In section 2 we, firstly, present the arguments leading Braham and Holler to deny the possibility of a preference-based power index. We then demonstrate why these arguments are not convincing. Section 3 deals with the argument put forward by Napel and Widgren that the SPI is not a true power index since it confuses power and luck. Section 4 addresses the question of whether the SPI can become negative. Section 5 is concerned with the Felsenthal and Machover proposition that the SPI is nothing but a modified Banzhaf index. Section 6 concludes the paper and presents our outlook.

## **2. Impossibility of the SPI?**

In this section, we deal with the critique put forward by Braham and Holler (2005) who argue that a preference-based power index is impossible. We, firstly, present the main argument leading Braham and Holler to deny the possibility of a SPI. Next, we discuss its main shortcomings.

### **2.1. A “Core Theorem of the Measurement of Power”**

Braham and Holler want to bring the “semantics of power into the centre of the debate about how to measure power” (Braham and Holler 2005: 139). By referring to the philosophical semantic analysis of power they take the notion of a “generic ability to effect outcomes” to be “the natural ‘fixed core of meaning’ of power” (Braham and Holler 2005: 145). In their words:

“If player  $i$  wanted a particular outcome or set of outcomes and that  $i$  has an action (or sequence of actions) such that the performance of these actions under stated or implied conditions will result in that outcome or set of outcomes and would not result if  $i$  would not perform this action (or sequence of actions), then player  $i$  would perform this action (or sequence of actions) and the specified outcome or set of outcomes would obtain. That is,  $i$  is essential or non-redundant for an outcome or set of outcomes” (Braham and Holler 2005: 145).

In the absence of that player’s intervention the state of the world would be different (Braham and Holler 2005: 145). Regarding simple games, one would speak of a swing (Braham and Holler 2005: 145, n. 8) or a player being decisive or pivotal.

From the definition of power as a capacity or potential to affect outcomes Braham and Holler conclude that a measure of power cannot accommodate any reference to the preferences of the players with respect to affecting outcomes. A power ascription is, firstly, categorical, secondly, “leaves the matter of what  $i$  wants undefined” and, thirdly, “does not say how much power  $i$  has,

only that there exist circumstances in which  $i$  is non-redundant for the outcome; a measure of power - power index – aggregates these ascriptions of non-redundancy in some way” (Braham and Holler 2005: 145-146).

The central claim of the article is formulated as “Core Theorem of the Measurement of Power”, which is, as the authors concede, not a theorem in the formal sense of the term, but rather “a kind of conceptual impossibility result that is germane to the theory of power generally” (Braham and Holler 2005: 138). The ‘theorem’ is stated in the following way:

“*Core Theorem of the Measurement of Power: If power is the ability of  $i$  to affect an outcome, then a measure of  $i$ 's power must exclude any reference to  $i$ 's preference (behavioural content) with respect to affecting that outcome*” (Braham and Holler 2005: 146).

Three reasons are given for this statement:

- “(1) being disinclined to do something does not imply the inability to do it;
- (2) psychological states such as desires and wants are not normally applied to the concept of ability; and
- (3) the *exercise* of an ability is not to be conflated with its *possession*” (Braham and Holler 2005: 146).

Braham and Holler are of the opinion that that a preference-based power index such as the SPI violates these three conditions: it conflates disinclination with inability (Braham and Holler 2005: 146-148); redefines the game form, since a “phobiafied” strategy, i.e. a strategy which is not rational being chosen, cannot be considered a strategy at all (Braham and Holler 2005: 148-150); commits the so called *exercise fallacy* by conflating the “*possession* of a disposition (*having* power) with its *exercise*” (Braham and Holler 2005: 151).

With regard to a game theoretical setting, Braham and Holler “derive” a corollary of their theorem, which

“states that a player’s power resides in, and only in, the strategies available to her given by the *game form* and not in the way that she plays the *game*. This implies that power is a value-independent concept. The upshot is that the Core Theorem renders unintelligible any attempt to formulate a measure of power in terms of the equilibrium of a non-cooperative game – the very idea of strategic power indices. Put bluntly, assessing how a player may play a game does not help us answer such questions as ‘Is Smith more powerful than Jones?’ or ‘What is the extent of Smith’s power?’ because power concerns what players may be *able to do*, not the actions they *may* or *do* take” (Braham and Holler 2005: 139).

Interestingly also to Braham and Holler power is linked to the game form and the strategies available to players. The SPI gathers information on the success of the various, available

strategies, which are embedded in the game form, by comparing the outcomes for a distribution of states of the world. Following a broad and general distribution basically levels out the effect of specific values related to preferences and policies, which seem to be the main reason of Braham and Holler's objection.

## ***2.2. Is there a Fixed Core of Meaning of Power? (Pitfalls of essential definitions)***

The essay of Braham and Holler is an exercise in semantics. They concede that they are “making liberal use of the philosophical semantic analysis of power conducted” (Braham and Holler 2005: 138), but they add: “It must not, therefore, be thought that we are refreshing old philosophical debates. Rather, we are bringing the *semantics* (italics added) of power into the centre of the debate about how to measure power“ (Braham and Holler 2005: 138). In fact, they claim having formulated the “right” (“true”) definition of power, with “general ability to affect outcomes” constituting its essence or intrinsic fundamental nature. In the philosophy of science those definitions are called “essential definitions”. The problems associated with essential definitions are well known (Popper 1960, Chapter I.10): Is there one, and only one, notion of power? How do we know that “general ability” is the essential property of power? How can we evaluate the definition in terms of the truth or falsity of the description given by it? Referring to “what we customarily mean by ability” (Braham and Holler 2005: 144) is a doubtful criterion, raising more questions than solving ones.

We should try to avoid converting substantial problems, for example matters of truth and falsity or policy recommendations, in purely verbal ones, since this paves the path for endless discourses, and we should reject the view that we should aim at and can obtain ultimate explanations by looking for essences. Following the path of methodological nominalism, definitions such as “power is a generic ability” should be read from right to left, as an answer to “What *shall* we call a generic ability in a game form?”, and not from left to right as an answer to “What *is* power in a game form?” Accepting this rule, one would be rather reluctant in conducting an “analysis of power per se”, as done by Braham and Holler (2005:154). Since we do not have a criterion for figuring out what “power per se” actually is, it seems reasonable to take an instrumental stance to the definition and to ask, “Which definition is helpful in answering scientific questions?”, and: “Why are we interested in a definition of power?” The answer clearly depends on where we want to use the term. Several possibilities come to mind: If power is part

of a theory, the explanatory power of the theory might depend on the definition. For normative statements, the workability or the empirical relevance of a concept of power in the sense of “What people are really interested in” might be decisive. From this perspective one might ask: Of what interest is it to know what a player is able to do, if it is not rational to do it? Why should we be interested in the potential or capacity of an action to alter outcomes if this does not is in accordance with equilibrium behavior?<sup>7</sup>

The upshot is that power can and should be defined in several ways – depending on the research question. In some contexts it might be useful to define power the way Braham and Holler did, i.e. applying the criterion of decisiveness, in others it is better to follow the SPI approach, which relies on the criterion of success. In section 2.3.3, we will show that in take-it-or-leave-it committees – these are the voting bodies to which the SPI is applied – the criterion of success is the better measure of power. In the next sections we illustrate the relevance of the above arguments by analyzing some well-defined games.

### ***2.3 Thinking Strategically vs. “Analysis of Power Per-se” or: Why the Inclusion of Preferences is Necessary***

Strategic interactions arise in two forms. The first is sequential. Here, players make alternating moves whereby earlier moves are observable to those choosing later. In a simultaneous game, players act at the same time in ignorance of the other player’s current actions (game of imperfect information).

#### 2.3.1 Constitutional Choice

Consider three legislators, A, B, and C, who must vote in alphabetic order under a majority rule, on whether to increase their own salaries (see Ordeshook 1992: 41 f.). Each legislator prefers to receive the pay raise, but each realizes that the constituents will not be pleased with a legislator voting to increase his own salary. There are four possible outcomes (see Ordeshook 1992: 41):

- "o<sub>1</sub>: The raise passes, but the legislator votes against it.
- o<sub>2</sub>: The raise passes, and the legislator votes for it.
- o<sub>3</sub>: The raise fails, and the legislator votes against it.
- o<sub>4</sub>: The raise fails, but the legislator votes for it."

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<sup>7</sup> See Barry’s critique of the Shapley-Shubik index (Barry 1980).

Let  $u$  denote utility, then the preferences of the legislators are summarized by the following numbers

$$u_i(o_1) = 2, u_i(o_2) = 1, u_i(o_3) = 0, u_i(o_4) = -1, \text{ with } i = A, B, C.$$

Figure 1 represents this voting situation in extensive form, where the terminal nodes are associated with the payoff 3-tuple  $(u_A, u_B, u_C)$ .

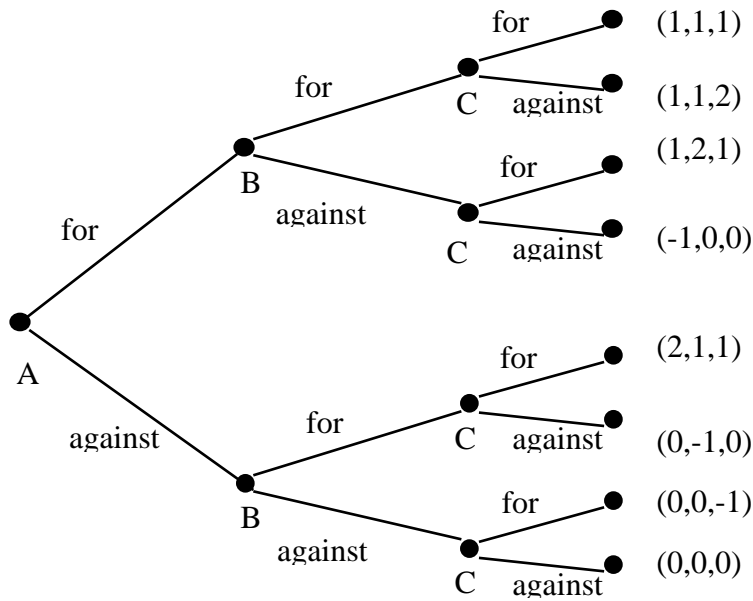


Figure 1: The pay-raise game in extensive form

A game form analysis of this voting game, i.e. neglecting the payoffs of the players, which applies „general ability to affect outcomes“ as indicator of „power per-se“ would reveal that each player has power: If two players were to vote differently the third one is decisive, he decides which state of the world obtains – pay-raise or status quo. Since this result holds for each player, traditional power indices would assign equal power values to each of the three players. However, the game is a sequential one, which matters a great deal.



Assume, society consists of our three players who had to choose, say, unanimously the game form underlying the game that is to be played afterwards.<sup>8</sup> Which game forms are candidates for getting unanimous support?

From the point of view of power as a „general ability to affect outcomes“ the game form of Figure 1 is a candidate. Power seems equally distributed – the sequential order of play does not matter. We doubt that players are so stupid not to see that the order of play is highly relevant. The legislators must vote alphabetically – player A is moving first, player B moving second and player C moves last. Player A enjoys a first mover advantage, which can be seen if we derive the subgame perfect equilibrium. The unique subgame perfect equilibrium is: (against, for, for). Player A receives the highest payoff (2), whereas the other players must content themselves with their second best outcomes. Note, if B and C were to change position the outcome of the game would not be affected. Clearly, each player would prefer to occupy the first mover position. A sequential game form such as in Figure 1 would only have a chance to be chosen on the constitutional level, if uncertainty exists with respect to the first mover position. In such a case, each player must form beliefs about his position. With a perfect veil of ignorance these beliefs would be identical, leading to identical expected utilities for the players, given the majority rule  $m = 2$ . Similar calculations are required for the  $m = 3$  and  $m = 1$  rules.

Having done all these computations, the players can choose, on the constitutional level, which rule is best for them – given a sequential setting. But why should a sequential game be chosen at all? On the constitutional level players are free to choose a simultaneous game, which would change the structure of information of the pay-raise game dramatically.

Figure 2 portrays this game in strategic form (see Ordeshook 1992: 45) ordering the payoffs (player C, player B, player A).

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<sup>8</sup> This is a traditional constitutional choice problem (Buchanan 1990). On the constitutional level, society must choose the rules (choice of rules) that govern decision-making on the post-constitutional level. On the post-constitutional level, choices have to be taken within the rules decided upon on the constitutional level.

|           |                    |                    |
|-----------|--------------------|--------------------|
|           | A for              | A against          |
|           | B for    B against | B for    B against |
| C for     | 1, 1, 1            | 1, 2, 1            |
| C against | 1, 1, 2            | -1, 0, 0           |

|           |                    |                    |
|-----------|--------------------|--------------------|
|           | A for              | A against          |
|           | B for    B against | B for    B against |
| C for     | 2, 1, 1            | 0, 0, -1           |
| C against | 0, -1, 0           | 0, 0, 0            |

Figure 2: Pay-raise game in strategic form

In contrast to the game portrayed in Figure 1, where players A, B, C have 2, 4, 16 strategies, respectively, in the simultaneous game the strategy sets B and C are identical to A's – to vote for or against. Here, player C cannot condition on the choice of player A or B and B cannot condition on player A's choice. This game has four Nash equilibriums: (A for, B for, C against), (A for, C for, B against), (A against, B for, C for), (A against, B against, C against). Thus, in this section we reached a conclusion similar to that in the previous section. The upshot is that a constitutional analysis, which restricts itself solely to the analysis of game forms, would be incomplete.

### 2.3.2 Inferior Players

Next, consider a 3-player simple game where the only winning coalitions are the grand coalition ABC and the two coalitions AB and AC (this example is from Napel and Widgrén 2001: 213; Widgren and Napel 2001: 1-2). Looking at this game as a coalitional form game the Banzhaf and Shapley-Shubik power vectors are  $(\frac{3}{5}, \frac{1}{5}, \frac{1}{5})$  and  $(\frac{2}{3}, \frac{1}{6}, \frac{1}{6})$ , respectively.

From the point of view of non-cooperative game theory – following Napel and Widgrén (2001: 213) – the game can be looked at as a sequential game, in which A makes, after flipping a coin, an ultimatum offer to B, asking for approval in return for an only marginal (and in the limit non-extent) concession to B's interest. A rational player B would have to accept the proposal, if a blocking coalition BC cannot be formed. B knows that if he rejects the proposal, A would move to C, who serves as a perfect substitute in forming a winning coalition. A similar reasoning holds in the case in which A makes the ultimatum offer to C. Thus, we would conclude, contrary

to what power measures based on coalitional form games indicate, B and C are powerless in this game. Napel and Widgren (2001: 213-4) call players that are robbed of their power commonly associated with their swing inferior players.

Indeed, application of the machinery of the strategic power index shows that B and C are powerless. Consider a policy space with three possible outcomes and identical distance, denoted  $\delta$ , between two neighboring outcomes; player set  $\{A, B, C\}$  and D as dummy player. This player is not a true player but rather an outside observer. The ideal points are uniformly distributed on the policy space. Figure 3 shows one of the feasible preference constellations.

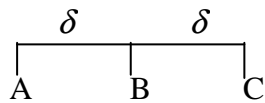


Figure 3: Preference constellation

Translating the notion of an ultimatum game to our setting means that, whatever the distribution of ideal points (preference profile) of players A, B, C, the policy outcome always corresponds to A's ideal point. Thus, A's power score  $\Psi_A = 1$ . Since we assumed that the probability distribution of D's ideal points is the same as those of B and C, D's expected distance equals those of B and C:  $\Delta_B = \Delta_C = \Delta_D$ . Thus,  $\Psi_B = \Psi_C = 0$ .<sup>9</sup> The upshot is that traditional power indices assign power scores to players without taking into account their position as inferior players. Thus, they neglect a factor that may be highly relevant from a player's point of view.

### 2.3.3 Agenda Setting versus Veto Power

Related to the first mover issue analyzed above is the problem of agenda setting power and veto power. Agenda setters are first movers, but not every first mover is an agenda setter. Classical power indices are not able to analyze and evaluate these distinctive types of power since all players are simply veto players. There are only two subsets of players, a 'winning' and a 'losing' one. Braham and Holler acknowledge that those indices are insensitive to the strategic aspects of power relations (Braham and Holler 2005: 141). They even illustrate this feature by two

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<sup>9</sup> Note the difference to the strict power index approach favoured by favoured Widgren and Napel, where A is not treated as a 'pure' ultimatum player. Whereas A's SPI score is 1, the strict power index is 5/7. However, according to both indices B and C are powerless.

elementary examples. In one of their examples they consider a committee of seven players with each player having one vote and a 5/7-majority rule (Braham and Holler 2005: 142-143). They further assume a preference configuration ranking the players in a one-dimensional policy space and a proposal falling from heaven. They show that not all coalitions are rationally feasible, and that not every swing will be exercised by a rational agent (Braham and Holler 2005: 142). However, despite acknowledging the intuitive appeal of the critique encapsulated in the examples, they are still having the opinion that “it is fundamentally mistaken. The reason hinges on a conceptual issue: what we mean by a power ascription” (Braham and Holler 2005: 143). A substantial problem is converted into a verbal one! In most of the committees we know of there are agenda setters, and it is well known that a specific type of power, different from the power of a veto player, is associated with the position of an agenda setter as a first mover. A power concept that systematically neglects the sequential structure of collective decision-making is unable to measure this type of power and to address the problems and their solutions associated with it.

To show why traditional voting power indices do not represent the distribution of power between an agenda setter and several veto players in a satisfactory and meaningful way, we choose, as a simple example, a decision-making procedure used in the European Union. With regard to legislative decision-making, the EC Treaty initially provided only for the unanimity version of the consultation procedure. This procedure allowed the Commission to propose new regulations or directives, which are subjected to unanimous consent by the Council. The latter implies that, in fact, each Council member has the right to veto the Commission’s proposal. The European Parliament only needs to be consulted in this procedure. Since the Council can adopt a proposal regardless of the position Parliament takes, Parliament does not play a significant role and thus will not be discussed further.

Now assume that policies can be represented by a one-dimensional (left-right) outcome space and players have Euclidean preferences. In addition, assume that players have perfect and complete information. The Commission selects a proposal, which is then decided upon by the Council members. For our argument on the usefulness of voting power indices, we assume that Council members are not allowed to add new proposals to the agenda or to amend the Commission proposal. The interactions between the Commission and Council members now resemble the well-known agenda-setter model of Romer and Rosenthal (1978, 1979).

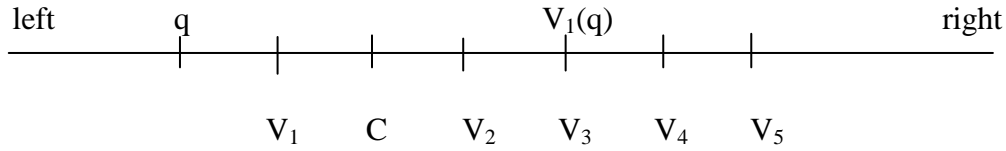


Figure 4: Preferences of the Commission and the Council Members

Figure 4 presents a preference configuration that may occur for the Commission, which is conceived as a unitary actor, and a five-member Council. In this Figure  $V_i$  and  $C$  denote the most preferred or ideal points of Council member  $i$  and the Commission, respectively, and  $V_i(q)$  stands for member  $i$ 's point of indifference to the status quo  $q$ . The Commission,  $C$ , has a more progressive preference than most Council members,  $V_i$ . Nevertheless, the leftmost Council member,  $V_1$ , holds an even more extreme position. Given a status quo to the left of these players, the Commission will propose a measure that is equivalent to its own most preferred point. Since all Council members prefer this point to the status quo, the proposal will not be vetoed. So, in equilibrium, the outcome of this game is a legislative policy  $x = C$ .

In this context, all players have to approve a measure, and no measure can be taken without the support of each one of them. Each (last) player has the same probability of being pivotal, and each player is necessary to form the (minimum) winning coalition of all players. The Shapley-Shubik, Banzhaf, Johnston and Holler indices therefore allocate power values of  $1/6$  to each player. These individual scores would suggest that the Commission is as 'powerful' as the Council members. The aggregated score of the Council would even be  $5/6$ , which implies that the Council would be *more* powerful than the Commission. However, the abilities of these players to affect the equilibrium outcome differ. The Commission can take the initiative and draft a proposal, while Council members can only approve or reject this proposal. Council members may restrict the Commission's policy choice, but they cannot set the final proposal. The Commission enjoys discretion in choosing a new policy, which makes it more 'powerful' than the traditional indices indicate.

Adding together the scores of individual Council members to calculate the power of the Council leads to what we call an *aggregation bias*. This bias is the result of the fact that, in

interbody analyses of voting power, the members of separate decision-making bodies are treated as if they were the members of a single committee. However, in the game as discussed, a proposal must be approved by both the Commission and the Council, regardless of the voting rule the Council uses to reach a collective decision. If the Commission does not belong to a coalition, then this coalition is not a winning coalition. Both players can be regarded as necessary players. Therefore, one would expect that both actors have power values of  $\frac{1}{2}$ , and not  $\frac{1}{6}$  for the Commission and  $\frac{5}{6}$  for the Council. The bias, as revealed by these numbers, leads to an exaggeration of the Council's abilities and an understatement of the power of the Commission. In addition, the power value of the Council, in a game with the Commission, is independent of the number of Council members. The individual values are only relevant to assess each member's power in shaping a Council decision and not a decision that has to be taken by several 'institutional' actors, including composite decision-making bodies.

#### **2.4 Strategic Power: Ability of Being Successful**

The SPI measures a player's ability/capacity/potential (whether generic or not) on average to influence (affect) as a member of a voting body the equilibrium outcome of a voting game or, in other words, the ability/capacity/potential "to get what you want" by incentivizing as a member among other members of a voting body an agenda-setter to present proposals which approach as close as possible the preferences of the respective player. It is an indicator of average success of affecting *equilibrium* outcomes.

This potential to affect equilibrium outcomes is determined by the game form, the state space and state variables (which are random variables). Taking into account the preferences of the players serves the purpose of determining rational behavior and to derive the equilibrium in a specific game.<sup>10</sup> Since the sole sources of power are the game form, the state space and the state variables we can fully subscribe to Braham and Holler's statement:

"Ordinarily speaking, a 'power' ascription refers to a person's ability: what a person is able to do. In the game theoretic context that we are discussing, the ability in question is to effect outcomes (i.e. 'force' or 'determine' outcomes) of the game. That is, a player has a strategy that, if chosen, will make a decisive difference to the outcome. *This basic definition is the same for a power index based upon a simple game and one that is ostensibly based upon a non-cooperative game* (italics added). The difference lies in the specification of the ability. In

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<sup>10</sup> Of course, our approach can also be applied to games of incomplete information, which would require making assumption regarding the possible types of players.

a simple game, the ability is turning a winning coalition into a losing coalition or vice versa, thereby being decisive for the acceptance or rejection of a bill, while, in a non-cooperative game, the ability is specified in terms of shifting the equilibrium in one's own favour" (Braham and Holler 2005: 143).

Note that in both models of a decision-making procedure the veto-players have identical action sets: they can either reject or accept a proposal. But only in the non-cooperative game setting players are assumed to act rational, i.e. choosing that action which leads to the better individual payoff.

It depends on the decision-making rule whether or not a player is *decisive* as for the equilibrium outcome. With a unanimity rule each veto player is decisive in the sense that the rejection or acceptance of a proposal always, i.e. whatever the preference configuration, depends on the action chosen. With a rule of simple majority there are sometimes preference configurations in which the equilibrium outcome of the game, i.e. either the status quo or, if there is a proposal, its content, crucially depends on the action of a player; but sometimes the equilibrium outcome is determined irrespective of the action chosen by a player. Nevertheless, in the latter case still distances between the ideal points and the equilibrium outcomes can be calculated and they are included in our power measure.

From the discussion above it should be obvious that, contrary to what Braham and Holler (2005: 147-148) believe, taking into account the state space and state variables in measuring a player's power does not mean conflating disinclination with inability. What the SPI measures is simply the ability/capacity/potential of a *rational player* to affect an (equilibrium) outcome, which is a subset of all possible outcomes. Finally, contrary to what Braham and Holler (2005: 150-152) believe, we do not conflate the possession of power with its exercise thereby committing the so-called exercise fallacy. What the players, the agenda-setter and the veto-players, do is exercising rational behavior. Whether or not, for example, a veto-player affects the equilibrium outcome depends on the decision-making rule and the rational behavior of all other players.

Meanwhile even adherents of the traditional power index approach question that there is only one notion of voting power, namely decisiveness. They realize that the notion of "satisfaction" or "success", "that is, focusing on the likelihood of having the result one voted for irrespective of whether one's vote was crucial for it or not" (Laruelle, et al. 2006: 186) is a meaningful notion of "voting power" and might be more relevant than decisiveness from the voters' point of view

(Laruelle, et al. 2006: 189; Laruelle et al. 2008). Whereas in so-called bargaining committees decisiveness is the adequate notion of power, in so called take-it-or-leave-it committees – these are the committees in which the set of players “is entitled only to vote for or against proposals submitted to it by an external agency” (Laruelle et al. 2008: 53) - success is the better one (Laruelle et al. 2008). We agree but there remains still a difference to our measure of success: Laruelle et al. measure success by a probability, whereas we take the expected distance between a player’s ideal points and the equilibrium outcomes.<sup>11</sup> But irrespective of this difference, what Laruelle et al. (2006: 201/203) conclude is worth to be quoted:

“Perhaps the fascination raised by the notion of ‘power’ has caused a distortion of focus in the field. It can be argued that decisiveness seems intuitively closer to the notion of ‘power’ than that of success, but this does not grant greater credit to recommendations based on this interpretation. In other words, the relevant question is not what notion is closer to the intuitive idea of ‘power’, but is a more adequate basis for normative recommendations. And as a base for normative recommendations (e.g., in connection with important issues, as that of the most adequate voting rule in a ‘take-it-or-leave-it’ committee of representatives) it seems more relevant the notion of success than that of decisiveness”.

The upshot of these deliberations is that a decision-making procedure can be modeled in several ways: as a simple game, using a coalitional or purely probabilistic approach, or as a non-cooperative game. Which one is superior depends upon the question to be addressed *and* whether or not the nature of the decision-making procedure, for example, the sequential moves of the players, the inter-body decision-making or the possibility to vote strategically (Schmidtchen and Steunenbergh 2002: 206-214), is adequately captured. To paraphrase Braham and Holler: “Here lies the heart of the problem” (Braham and Holler 2005: 144).

### **3. The SPI: Confounding Power with Luck?**

In a much-cited paper entitled „Is it Better to be Powerful or Lucky?” Brian Barry presented the following formula: success = luck + decisiveness (Barry 1980: 338). Although Barry had not been concerned with non-cooperative voting games and, moreover, defined the terms as probabilities, the logic of this formula applies in a modified way to the SPI as well. The modification consists in substituting, firstly, probabilities by distances between ideal points and equilibrium outcomes, and, secondly, decisiveness by strategic power. As for the latter substitution, recall that power has nothing to do with decisiveness but refers to the ability of

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<sup>11</sup> Another difference is worth to be mentioned: Whereas in the Laruelle et al. model proposals are submitted by an external agency, the agenda setter in our model is a player, thinking strategically.



getting desired (equilibrium) outcomes. In order to level out the effect of luck, we focus on the average or expected ability.

This procedure has been criticized by authors who are in favor of power indices quite similar to ours. For example, Napel and Widgrén propose – as we do – a unified framework for measuring power as determined by spatial preferences, strategic agenda setting and decision-making procedures (see Napel and Widgrén 2004). Thus, they do not deny the possibility of a preference-based power index. However, they claim that the framework underpinning the SPI leads to a *strategic success index*, rather than a strategic power index. In their view, SPI measures „the ability of a player to make a difference in the outcome“, i.e. power, only under very special circumstances (Napel and Widgren 2004: 524): „Unless one regards average success as the defining characteristic of power (which neither Steunenberget al. nor many others do), taking expectations will only by coincidence achieve what Steunenberget al. aim at, namely, to level out the effect of ‚luck‘ or a particular preference configuration on the outcome of a game‘ (p. 362)“ (Napel and Widgren 2004: 524). Napel and Widgren concede that the SPI „is a good measure of average success but, in general, it fails to capture power“ since the SPI confounds luck with power (Napel and Widgren 2004: 524).

We will discuss this critique in turn. Consider Figure 4, which can be used to illustrate the importance of distinguishing ‘power’ from ‘luck’. The equilibrium outcome of the game is  $x = C$ , that is, the most preferred position of the Commission. This outcome seems to be more favorable to Council member 2 than member 5, since the distance to  $V_2$  is less than the distance to  $V_5$ . Is member 2 therefore also more powerful? Both players have the same abilities to affect the outcome, that is, to veto the Commission proposal. So, from this perspective, there is no difference in power. Nevertheless, the outcome is closer to member 2’s preferences. This indicates that member 2 is more ‘lucky’ than member 5. Having a preference that lies close to the equilibrium outcome of a particular game does not necessarily mean that this player is also ‘powerful’. Similarly, one may question whether Council member 1 is more ‘powerful’ than the other Council members, since this player defines the boundary,  $V_1(q)$ , where the Commission can no longer select its ideal point, should this player move to the right. If any other player can also occupy the position of this member, or the status quo can be located at any other point along the policy dimension, Council member 1 is just more ‘lucky’ than the others. Following Barry (1980), we regard a player’s *success*, which is defined as the extent to which the outcome of the

decision-making process corresponds to its ideal point, as the composite effect of ‘power’ and ‘luck’. Part of a player’s success is therefore based on ‘luck’, the other part is due to the ‘power’ a player exerts.<sup>12</sup>

Whereas power can be associated with a player’s ability to affect the final outcome (which is basically a matter of the rules of the game telling us *who* can do *what* and *when* and who gets *how much* when the game is over (see Binmore, 1992: 25)), ‘luck’ is related to the preferences of the players and the location of the status quo, which are assumed to be exogenously determined. The latter can be illustrated by the role of the Commission in our example of the consultation procedure. The fact that the outcome of the game coincides with the Commission’s most preferred point does not imply that the other players in the game are ‘powerless’. This result depends on the preferences of the Council members and the location of  $q$ . A shift of  $V_1$  to the left may, for instance, force the Commission to propose a policy  $x = V_1(q)$ . Thus, given the preference configuration, the Commission is ‘lucky’ that Council members have preferences that allow for the equilibrium outcome  $x = C$ . This clearly indicates that the *success* of a player in a given game is the combined result of *abilities* (defined by the rules of a game) and the specific *preference configuration*. To assess a player’s power, a measure should be based on the former and not the latter.

To distinguish ‘power’ from ‘luck’, we propose a measure that is independent of the preferences of players in a specific game, which, together with the decision-making procedure, determines the outcome of the game. This can be achieved by measuring a player’s power under some decision-making procedure with reference to the *mean* or *expected* distance between the equilibrium outcome and this player’s ideal point for all possible combinations of players’ preferences and all possible combinations of the status quo. In doing so, the power-luck

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<sup>12</sup> Note the difference between our definition and Barry’s definition, which has recently been given more precision by Laruelle and Valenciano (2008: 54-55, 58). In their view a player is successful *ex post*, i.e. once the players have voted on a given proposal, if he/she obtains an outcome – acceptance or rejection of a proposal – that he/she has been voted for. A voter has been decisive if he/she is successful and his/her vote was crucial (critical) to that outcome. Luck is simply success without decisiveness, i.e. a player’s vote is irrelevant for the outcome. Thus, Laruelle and Valenciano interpret decisiveness, success and luck as binary variables. Our definition of terms is more general than Laruelle and Valenciano’s, firstly, in that it refers not only to veto-players but also includes the agenda-setter. Secondly, in our framework, a player is successful if his/her vote influences the content of the proposal such that the equilibrium outcome moves towards his/her ideal point (including the case in which the status quo remains). Contrary to Laruelle and Valenciano, in our framework a player can be more or less successful, since the distance between the equilibrium outcome and a player’s ideal point can vary.

confusion vanishes. The fact that our power scores turned out to be sensitive to a change of the decision-making procedures (all other things being equal) gives further support to this conclusion.<sup>13</sup>

#### 4. The SPI: Can it Become Negative?

Napel and Widgren claim that the SPI may become negative (Napel and Widgren 2004: 524; 2002: 9-10). If so, the SPI would be a strange construct since attributing negative power to a player does not make sense. Fortunately, it can be shown that Napel and Widgren's claim is based on assumptions not in accordance with our approach. We discuss two examples Napel and Widgren developed in support of their claim (Napel and Widgren 2002: 9-10; 2004: 524).

Consider a simple majority voting game with three players having equal voting weight and outcome space  $X = \{-1, 0, 1\}$ . Player 1's random ideal point,  $\lambda_1$  is degenerate and always equal to 0, whereas the ideal points of players  $i = \{2, 3\}$ ,  $\lambda_i$ , are uniformly distributed on  $X$ . The status quo is fixed on position 0. In only two out of nine states of the world  $\xi = (q, \lambda_1, \lambda_2, \lambda_3)$  with  $q = 0, \lambda_1 = 0$ , and either  $\lambda_2 = \lambda_3 = -1$  or  $\lambda_2 = \lambda_3 = 1$  the status quo does not prevail. Since average distance is  $2/9$  for player 1 and  $4/9$  for both other players, player 1 appears to be the most successful and most powerful player. Napel and Widgren (2002: 10) conclude: „However, exactly the same equilibrium outcomes prevail when player 1's voting weight is reduced to zero, i.e. if he becomes a dummy player“ (assuming that for an even number of players the status quo wins unless defeated by a majority). And they add: „According to Steunenberget al.'s Strict Power Index, he is still the most powerful player“.

There got something wrong in this exercise, and it is easy to figure out what. Given that the status quo is always  $q = 0$  and the ideal point of player 1,  $\lambda_1$ , is supposed to be always at the status quo, the set up of the game implies a status quo bias. Therefore it is not surprising to see player 1 coming out as the most „powerful“ player. This status quo bias still exists if player 1 has a voting weight of zero, since a majority, in fact unanimity, is needed to defeat it. Player 1 is clearly in both scenarios the most successful player, but not the most powerful. His/her superior

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<sup>13</sup> Note again the difference between our approach and that proposed by Laruelle and Valenciano (2008: 58). They define the *ex ante version* of the three terms success, decisiveness and luck (irrelevance) using probabilities. The probability of a player being decisive is simply the difference between his/her probability of being successful minus the probability of being lucky.

performance is due to a restriction of the set of possible states of the world from 81, under the assumptions we would use to calculate the index, to 9, leading to luck for player 1 and bad luck on the side of players 2 and 3.

The SPI is normalized by the introduction of a dummy player. Contrary to Napel and Widgren's approach, this player is not a true player but rather an outside observer. In fact, by assuming player 1 being a dummy player Napel and Widgren transform the three-player game into a two-player game.

We define a dummy player as „a player whose preferences vary over the same range as the preferences of the actual players, but that has no decision-making rights in the game“ (Steunenberg et al. 1999: 348). Napel and Widgren claim that this definition of a dummy player is not always meaningful:

„What does it mean to ‚vary over the same range‘ if the so-called actual players' ideal points (to stay in a spatial voting framework) have different supports; e.g.  $\tilde{\lambda}_i$  is uniformly distributed on  $[0, 1]$  and  $\tilde{\lambda}_j$  has triangular distribution on  $[1/2, 4]$ ?“ (Napel and Widgren 2002: 11).

The answer is that the expression „same range“ refers to the range in the policy space in which the ideal points of *all* players can be distributed. In the example given by Napel and Widgren it is the range  $[0, 4]$ .

Next, consider the second example developed by Napel and Widgren with the purpose to illustrate that, contrary to our view (Steunenberg et al. 1999: 349, n. 7), „equilibrium outcomes can be systematically biased against the interest of a particular player“ (Napel and Widgren 2002: 11). If so, the SPI can become negative. In a group of four boys, the oldest one is the agenda setter and makes proposals as for what to do in the afternoon. Proposals have to be accepted by a majority of the remaining three boys. All boys have independent preferences, which follow the same distribution. According to the SPI framework the oldest boy as agenda setter is the most powerful player, and the SPI value is the same for the remaining players. There is a little brother of the oldest boy who is allowed to participate in the afternoon activities of the group but does not have a say in selecting the program. Regarding its preferences Napel and Widgren (2002: 10) make the following crucial assumption:

“It is plausible to assume that he does not always agree with his elder brother's most desired outcome, but does so more often than with the others' ideal alternatives. Mathematically

speaking, let the ideal points of the two brothers be positively correlated. Then, the mean distance between the group's equilibrium activity and its youngest member's most desired recreation will be smaller than that of those group members who actually have their vote on the outcome".

Of course, this conclusion does not come as a surprise. Despite the fact that little brother does not have a say in the game he is *not* a dummy player in the sense we defined the term. He is simply lucky to have a preference closely related to that of the player that is most powerful. This is also the reason why the SPI would *not* assign power to Luxembourg, to take another example referred to by Napel and Widgren (2002: 11). Luxembourg is lucky having similar views with the other Benelux countries.

The lesson to be learned from the above exercises is that the type of „dummynization“ as well as the choice of the probability distribution of ideal points on the domain of the outcome space matter a lot. The SPI can only become negative in settings, in which luck is mistakenly interpreted as power. The following conjecture seems to be reasonable: Given a policy space and a given number of players, the smaller the set of feasible states of the world, the less can luck be leveled out by taking expectations and the more is the SPI converted into a strategic success index.

The same holds regarding modifications of the probability distribution on the domain of the outcome space: „Only for particular distribution assumptions is luck ‚leveled out‘ by taking averages“ (Napel and Widgren 2004: 524). We agree, but we would maintain that the probability distribution that we applied is the one which approximates the idea of „a priori“-ness the best. Following Felsenthal and Machover (2001: 94), „to obtain an a priori strategic measure we must go behind a veil of ignorance: we must minimize the information built into the state space and the distribution of the state variables“. The crucial question then is: what is the proper assumption regarding the distribution of the ideal points and the status quo? We feel that the veil of ignorance means that there is no information about the players' preferences and the status quo. Therefore, the principle of insufficient reason requires assuming that the state variables are mutually independent and uniformly distributed on the state space.<sup>14</sup> With the knowledge about the distribution of preferences and the status quo assumed by Napel and Widgren in their

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<sup>14</sup> We agree with Felsenthal and Machover (2001: 94) that this is not sufficient, „because the geometric structure of the state space itself also carries some information. In particular, any asymmetry of this space implies a bias in favour of some states and against others“.

examples developed to show that the SPI can become negative, it is meaningless to take our index as a strategic power index. It is all *a posteriori*.

## 5. The SPI: A Banzhaf in Disguise?

In their comment on the ‘Symposium Power Indices and the European Union’ in the *Journal of Theoretical Politics* Felsenthal and Machover argue that strategic power is simply the Banzhaf power multiplied by a constant that depends on the shape of the state space (see Felsenthal and Machover 2000). If Felsenthal and Machover’s conclusion were correct we would take this as support for our view that the SPI is a possible and reasonable measure of power. In the following we, firstly, present a sketch of the Theorem proven by Felsenthal and Machover, which is then followed by an evaluation of the results.

### 5.1. The Theorem

Consider a simple voting game  $W$ . Let  $S$  denote a state space, which is totally symmetric.  $X_i, \dots, X_n, Y, Z$  are independent random variables, all of which take their values in the state space.  $X_i, Y, Z$  stand, respectively, for the ideal point of player  $i$ , the state if a proposed bill will be passed, and the status quo (i.e. the state that continues to prevail if the policy proposal is defeated).

Let  $R$  and  $r$ , respectively, denote the greater and smaller of the two distances  $|X_i - Y|$  and  $|X_i - Z|$ . Then the distance can be defined as

$$D_i = (1 - p) \cdot R + p \cdot r,$$

with  $p$  the probability that  $i$ ’s voting decision agrees with the outcome of the vote.

Using Penrose’s theorem, which state

$$p = \frac{1 + \beta'(W)}{2},$$

with  $\beta'[W]$  the Banzhaf, one can define the mean value of  $D_i$ , denoted  $\Delta_i[W]$ ,

$$\Delta_i[W] = \frac{1 - \beta'[W]}{2} \cdot R + \frac{1 + \beta'[W]}{2} \cdot r,$$

for player  $i$ , and

$$\Delta_d[W] = \frac{R + r}{r}$$

for the dummy player. This gives

$$\Psi_i[W] = \frac{R-r}{R+r} \cdot \beta'_i[W].$$

Felsenthal and Machover (2001: 95) conclude:

“Thus  $\Psi_i[W]$  is simply the  $B_z$  power of  $i$  multiplied by a constant that depends on the shape of  $\mathbf{S}$ . Note, in particular, that in the simplest possible case, where  $\mathbf{S}$  consists of just two points,  $r$  is clearly 0, so in this case  $\Psi_i[W] = \beta'_i[W]$  exactly. In our view, this result vindicates the  $B_z$  measure: not for the first time, a new approach to the measurement of a priori I-power has, yet again, led to  $\beta'$ . It also suggests that the strategic measure proposed by SS&K is a natural generalization of a priori I-power, which allows the incorporation of additional information, and thus the study of a posteriori voting power.”

Felsenthal and Machover believe that our method of measuring power is a promising candidate for a unified approach (Felsenthal and Machover 2001: 96). Since the SPI not only depends on the set of voters and the decision-making rule but also on the choice of the state space and the joint distribution of the state variables, there exists

“an enormous latitude for building into the model all kinds of information concerning the actual state of the world, the kinds of bill to be put to the vote and affinities or disaffinities between voters” (Felsenthal and Machover 2001: 93).

## 5.2. *Evaluation*

We welcome the Felsenthal and Machover approach. It forms a very interesting foundation of the approach presented here, which would allow the SPI to be fully characterized by the set of the axioms the Banzhaf is founded on. This axiomatic characterization would facilitate comparisons with other power measures. Although the theorem proved by Felsenthal and Machover provides for important insights into the logic of the SPI, three comments seem in order.

First of all, we agree that Felsenthal and Machover succeeded in reformulating the algorithm of the SPI as far as simple voting games are concerned. Simple voting games take the proposals to be voted upon as exogenously given. Thus, they can be treated – as in Felsenthal and Machover – as a random variable. However, the most important feature of the SPI namely the strategic interaction and the procedural constraints are not taken into account (see also Napel and Widgren 2002: 12-13; 2004: 524): the bills proposed in the SPI framework are not randomly chosen but are the result of strategic thinking along the subgame perfect equilibrium path.

To illustrate, consider Figure 4. We know already, in equilibrium, the outcome of this game is a legislative policy  $x = C$ . Here, the outcome of a specific sequential game is partly due to the value of the random variables and partly the result of strategic thinking on the side of all players. It is natural to think about how to introduce this factor in the Felsenthal and Machover set up. One could take account of strategic thinking by restricting the domain of proposed bills in the state space. The question is whether we can find some reasonable equivalent to the equilibrium concept used in non-cooperative game theory. On the other hand, one might conjecture that since proposals depend on the state of the world, including the ideal points of the Commission, and since the state of the world is a probabilistic variable, also the proposals are. In fact, one might even be tempted to apply the terms winning and losing coalitions in the context of a non-cooperative model of a decision-making procedure.<sup>15</sup> If a majority of the players vote in favor of a proposal then one could say that they form a „winning coalition“. However, one should speak of a „quasi-coalition“ since, as Felsenthal and Machover (2001: 84) rightly mention, „the very term ‚coalition‘, as referring to an arbitrary set of voters, is perhaps somewhat misleading, as it seems to imply conscious coordination“. Moreover, contrary to traditional power indices, the SPI takes account of the fact that the propensity to present a proposal and its content depends on the composition of potential winning coalitions. In other words: The agenda setter is looking for a winning coalition such that the distance between its ideal point and the proposal (generating a winning coalition) is smaller than the distance between its ideal point and the status quo. If there is no such a winning coalition the agenda setter remains silent.

Second, Felsenthal and Machover are of the opinion that the strategic power measure "is a natural generalization of a priori I-power, which allows the incorporation of additional information, and thus the study of a posteriori voting power" (Felsenthal and Machover 2001: 95). The notion of I-power is that of „power as *influence*: a voter's ability to affect the outcome of a division of a voting body – whether the bill in question will be passed or defeated“ (Felsenthal and Machover 2001: 84). They argue that the notion of I-power „has essentially nothing to do with cooperative game theory or, for that matter, with game theory generally, as it is normally understood. According to this notion, voting behaviour is motivated by *policy seeking*. The action of a given voter does not depend on what other voters may be expected to

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<sup>15</sup> As done by Widgren and Napel (2001) and Napel and Widgren (2004). See also the discussion in subsection 2.3.2.



do, let alone on bargaining and concluding binding agreements with them...Each voter simply votes for or against a given bill on what s/he considers to be the merit of this bill; and the way s/he votes is independent of the decision rule. The passage or failure of a bill is here best regarded as a public good (or public bad), which affects all voters, irrespective of how they have voted on that bill“ (Felsenthal and Machover 2001: 84).

We agree with Felsenthal and Machover that the SPI has nothing to do with cooperative game theory, but we disagree with Felsenthal and Machover’s characterization of the SPI as not being in essence a game theoretic concept. First of all, although in a simple voting game the action of a given voter does not depend on what other voters may be expected to do, it depends on what the agenda setter has done. Secondly, the action of the agenda setter clearly depends on what s/he expects the other players will do (backwards induction). Thirdly, application of the SPI approach is not restricted to simple voting games but has been applied to interbody decision-making (Steunenberg et al. 1999; Schmidtchen and Steunenberg 2002). Furthermore, in models allowing for the possibility of negotiating, amending or modifying proposals, forming coalitions and linking decisions on different proposals there is even more room for strategic considerations. Finally, the reformulation of the strategic power index, as presented by Felsenthal and Machover, is based on payoffs, since one cannot calculate differences without knowing the ideal points for all players. In fact, the constant with which the Banzhaf index has to be multiplied is a payoff measure. It is implicitly assumed that voters care about distances and that decisions are (rationally) determined by the distance of the ideal point from both the proposed bill and the status quo. These distances are utility measures.

In a comment on our 2002 article Moshe Machover takes up the issue that the distances in the state space can be interpreted as some kind of payoff contradicting the proposition that the SPI is not in essence a game theoretic concept (Machover 2002: 226-227). He thinks „that the contradiction is only apparent, not real“ (Machover 2002: 227). This belief follows from his characterization of the model underpinning the calculation of the SPI as consisting of two distinct parts: „The first part is a decision rule, a so-called ‚simple’ game or ‚simple voting game’. The second part consists of a state space and state variables (which are random variables). The decision rule operates in the conventional way: it tells us how the outcome of a division is determined by the way each of the voters vote. The second part of the model serves to model the motivation that leads each of the voters to vote in a particular way“ (Machover 2002:

225). Although Machover is right in identifying the two distinct parts, he neglects the crucial fact that the second part not only serves to model the incentives of the voters but also the strategic choice of the agenda setter. Moreover, although Machover explicitly concedes that the geometry of the state space and the distribution of the state variables *is* game theoretic, belongs to non-cooperative game theory and the voters' decision „*may well* be based on a calculation of expected payoff“ (Machover 2002: 227), he nevertheless sticks to his position that the model is not game theoretic: „The point is that in the case of I-power ... these motivations and payoffs are exogenous to the decision rule. This is precisely the situation in S&S's model: the decision rule resides in one part of the model, while the motivations and payoffs reside in the other part“ (Machover 2002: 227). True, but we cannot see why this ubiquitous feature of models, i.e., consisting of several parts which are conceptually different, deprives the SPI of its game theoretic nature. A good model integrates different parts such that new insights are generated.

Finally, we share Moshe Machover's position

„that a correct method of measuring actual voting power should be organically connected with the method of measuring a priori power. The reason for this is that actual power is the result of a superposition of real-life factors (such as preferences) on the ‚bare‘ decision rule itself. S&S's two-part model does precisely that; and when the contribution of the second part is reduced to nothing, the result is the Penrose measure“ (Machover 2002: 225-226).

However, reducing the second part to nothing would mean eliminating any strategic element in a power measure. The constant in the formula derived by Felsenthal and Machover simply disappear.

## **6. Conclusion**

In this paper we have discussed the critique raised against the SPI as a preference-based power index. Overall, we find that the critique is unfounded: Firstly, the proposition that the SPI is impossible results from playing with semantics. Secondly, the SPI does not confound power with luck, since taking expectations eliminates luck. Thirdly, properly calculated, i.e., taking the veil of ignorance concept seriously, it cannot become negative. Fourthly, the attempt to show that the SPI is nothing but a modified Banzhaf and, for this reason, is not game theoretic should be welcomed, since it takes preferences into account and supports our claim for a unified approach to the study of a priori and a posteriori (actual) voting power. However, it neglects any strategic interaction and important procedural features such as, for example, the sequential nature of the

game. Voting does not take place in an institutional vacuum. Rules of order exist, which determine the type of proposals or amendments that can be made, and the agenda of the voting process that must be used. Moreover, the voting body may use a committee structure, in which committees – or subsets of voters – discuss and reformulate proposals before they are put to a final vote on the floor. Not only the vote as such, but also these structures determine the extent to which individual players are able to affect the outcome of a vote.

The SPI refers to the ability of a player to make a difference in the outcome of a policy game. This index has many desirable features. First, it can be based on a careful and detailed analysis of some decision-making process in which the preferences of all players and all relevant institutional complexities are taken into account. Second, like traditional voting power indices, the strategic power index measures *a priori* power. However, in contrast to these indices the strategic power index provides a unified method to study the composite edifice of *a priori* and *a posteriori* power as a whole.

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